Parallelograms Exercise 16A

What is a Parallelogram?

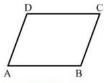
- Opposite sides are parallel
- Opposite sides are congruent
- Opposite angles are equal
- Consecutive angles supplementary
- Diagonals bisect eachother

Туре	Properties
Parallelogram	Opposite sides are equal and parallel Opposite angles are equal
Rectangle	Opposite sides are equal and parallel All angles are right angles (90°)
Square	Opposite sides are parallel All sides are equal All angles are right angles (90°)
Rhombus	Opposite sides are parallel All sides are equal Opposite angles are equal Diagonals bisect each other at right angles (90°)
Trapezoid	One pair of opposite sides is parallel
Kite	 Two pairs of adjacent sides are equal One pair of opposite sides are equal One diagonal bisects the other Diagonals intersect at right angle (90°)

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Q1
 Answer:
 It is given that ABCD is a parallelogram in which \angle A is equal to 110°.
  Sum of the adjacent angles of a parallelogram is 180°.
   \therefore \angle A + \angle B = 180^{\circ}
  \Rightarrow 110^{\circ} + \angle B = 180^{\circ}
  \Rightarrow \angle B = (180^{\circ} - 110^{\circ})
  \Rightarrow \angle B = 70^{\circ}
  ∴ ∠B = 70°
 Also, \angle B + \angle C = 180^{\circ}
  \Rightarrow 70^{\circ} + \angle C = 180^{\circ}
  \Rightarrow \angle C = (180^{\circ} - 70^{\circ})
  \Rightarrow \angle C = 110^{\circ}
   \angle C = 110^\circ
  Further, \angle C + \angle D = 180^{\circ}
  \Rightarrow 110^{\circ} + \angle D = 180^{\circ}
  \Rightarrow \angle D = (180^{\circ} - 110^{\circ})
  \Rightarrow \angle D = 70^{\circ}
  ∴ ∠D = 70°
Q2
 Answer:
 Let the required angle be x^{\circ}.
 As the adjacent angles are equal, we have:
    x + x = 180
                                (since the sum of adjacent angles of a parallelogram is 180°)
  \Rightarrow 2x = 180
  \Rightarrow x = \frac{180}{2}
  \Rightarrow x = 90^{\circ}
 Hence, the measure of each of the angles is 90°.
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Q3

Answer:



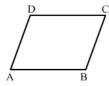
Let ABCD be the parallelogram.

Then, $\angle A$ and $\angle B$ are its adjacent angles.

Let
$$\angle A = (4x)^{\circ}$$

$$\angle B = (5x)^{\circ}$$

Q4



Let ABCD be a parallelogram.

 $L \text{ et } \angle A = (3x-4)^{\circ}$

 $∠B = (3x + 16)^{\circ}$ ∴ $∠A + ∠B = 180^{\circ}$ [s ince the sum of adjacent angles of a parallelogram is 180°]

 $\Rightarrow 3x - 4 + 3x + 16 = 180$

 $\Rightarrow 3x - 4 + 3x + 16 = 180$

 $\Rightarrow 6x + 12 = 180$

 $\Rightarrow 6x = 168$

 $\Rightarrow oldsymbol{x} = rac{168}{6}$

 $\Rightarrow x = 28$ $\therefore \angle A = (3 \times 28 - 4)^{\circ}$

 $=(84-4)^{\circ}$

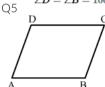
 $= 80^{\circ}$ $\angle B = ((3 \times 28) + 16)^{\circ}$

 $-(94 + 16)^{\circ}$

 $= (84 + 16)^{\circ}$ = 100°

The opposite angles of a paralleleogram are equal.

 $\therefore \angle C = \angle A = 80^{\circ}$ $\angle D = \angle B = 100^{\circ}$



Let ABCD be a parallelogram and let the sum of its opposite angles be 130°.

 $\angle A + \angle C = 130^{\circ}$

T he opposite angles are equal in a parallelogram.

 $\therefore \angle A = \angle C = x^{\circ}$ $\Rightarrow x + x = 130$

 $\Rightarrow 2x = 130$

 $\Rightarrow x = \frac{130}{2}$

 $\Rightarrow x = 65$

 $\therefore \angle A = 65^{\circ} \text{ and } \angle C = 65^{\circ}$

 $\angle A + \angle B = 180^{\circ}$ [since the sum of adjacent angles of a parallelogram is 180°]

 \Rightarrow 65° + $\angle B = 180$ °

 $\Rightarrow \angle B = (180 - 65)^{\circ}$

 $\Rightarrow \angle B = 115^{\circ}$ $\angle D = \angle B = 115^{\circ}$

റ്റ Answer :

Let the lengths of two sides of the parallelogram be 5x cm and 3x cm, respectively.

opposite angles of parallelogram are equal

Then, its perimeter = 2(5x + 3x) cm

=16x cm

 $\therefore 16x = 64$

 $\Rightarrow x = \frac{64}{16}$

→ m — 4

 \therefore One side \Rightarrow (5 × 4) cm = 20 cm Other side \Rightarrow (3 × 4) cm = 12 cm

07

Answer:

Let the lengths of two sides of the parallelogram be x cm and (x+10) cm, respectively.

Then, its perimeter = 2[x + (x + 10)] cm

= 2[x + x + 10] cm

= 2[2x + 10] cm= 4x + 20 cm

1.00 1.40

4x + 20 = 140 $\Rightarrow 4x = 140 - 20$

 $\Rightarrow 4x = 120$

 $\Rightarrow x = \frac{120}{4}$

 $\Rightarrow x = \frac{1}{4}$ $\Rightarrow x = 30$

Length of one side = 30 cm

Length of the other side \Rightarrow (30 + 10) cm = 40 cm

Answer:

Refer to the figure given in the book.

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In \triangle BMC and \triangle DNA:

\angle DNA = \angle BMC = 90^{\circ}

\angle BCM = \angle DAN (alternate angles)

BC = DA (opposite sides)

By AAS congruency criteria:

\triangle BMC \cong \triangle DNA

Yes, it is true that BM is equal to DN.

(by corresponding parts of congruent triangles BMC and DNA)
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Q9

Refer to the figure of the book.

$$∠A = ∠C$$
 (opposite angles of a parallelogram are equal)

⇒ $\frac{1}{2}∠A = \frac{1}{2}∠C$

=> $∠EAD = ∠FCB$ (AE and CF bisect the angles A and C , respectively)

In $△ADE$ and $△CBF$:

 $∠B = ∠D$ (o pposite angles of a parallelogram are equal)

 $∠EAD = ∠FCB$ (o pposite sides of a parallelogram are equal)

 By AAS concruency criteria:

 $△ADE \cong △BCF$
 $DE = BF$ (c orresponding parts of congruent triangles)

 $CD = AB$ (o pposite sides of a parallelogram are equal)

Also, $CD - DE = AB - BF$

⇒ $CE = AF$
 $ABCD$ is a paralleleogram.

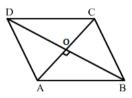
∴ $CD \parallel AB$ (o pposite sides of a parallelogram are parallel)

If one pair of sides of a quadrilateral is parallel and equal, then it is a parallelogram. Therefore, AECF is a parallelogram.

∴ AE || CF

Q10

Answer:



Let ABCD be a rhombus.

Let AC and BD be the diagonals of the rhombus intersecting at a point O.

Let AC = 16 cm

BD = 12 cm

We know that the diagonals of a rhombus bisect each other at right angles.

∴
$$AO = \frac{1}{2}AC$$

$$= \left(\frac{1}{2} \times 16\right) \text{ cm}$$

$$= 8 \text{ cm}$$
 $BO = \frac{1}{2}BD$

$$= \left(\frac{1}{2} \times 12\right) \text{ cm}$$

$$= 6 \text{ cm}$$

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From the right \triangle AOB:
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$$AB^{2} = AO^{2} + BO^{2}$$

$$= \{(8)^{2} + (6)^{2}\} \text{ cm}^{2}$$

$$= (64 + 36) \text{ cm}^{2}$$

$$= 100 \text{ cm}^{2}$$

$$\Rightarrow AB = \sqrt{100} \text{ cm}$$

$$= 10 \text{ cm}$$

Hence, the length of the side ABis10 cm.

$$AB = BC = CD = DA = 10$$
 cm (all sides of a rhombus are equal)

011

Answer:

Refer to the figure given in the book.

In $\triangle ADC$:

$$DA = DC$$
 (all sides of a square are equal)
 $\Rightarrow \angle ACD = \angle CAD$
Let $\angle ACD = \angle CAD = x^{\circ}$ [Angle opposite to the equal sides are equal]

Let $\angle ACD = \angle CAD = x^*$ [Angle opposite to the equal sides are equal] x + x + 90 = 180 [since the sum of the angles of a triangle is 180°]

$$\Rightarrow 2x + 90 = 180$$

$$\Rightarrow 2x = 90$$

$$\Rightarrow x = \frac{90}{2}$$

$$\Rightarrow x = 45$$

$$\therefore \angle CAD = 45^{\circ}$$

012

Answer:

Let the length of two sides of the rectangle be 5x cm and 4x cm, respectively.

Then, its perimeter = 2(5x + 4x) cm

$$= 18\mathbf{x} \text{ cm}$$

$$\therefore 18\mathbf{x} = 90$$

$$\Rightarrow x = \frac{90}{18}$$

 $\Rightarrow x = 5$ Length of one side $\Rightarrow (5 \times 5)$ cm = 25 cm

Length of the other side \Rightarrow (4 × 5) cm = 20 cm

 \therefore Length of the rectangle = 25 cm

Breadth = 20 cm

Q13

Answer:

- The diagonals are equal and the adjacent sides are unequal. Hence, the given parallelogram is a rectangle.
- (ii) The diagonals are equal and the adjacent sides are equal. Hence, the given parallelogram is a square.
- (iii) The diagonals are unequal and the adjacent sides are equal. Hence, the given parallelogram is a rhombus.
- (iv) All the sides are equal and one angle is 60°. Hence, the given parallelogram is a rhombus.
- (v) All the sides are equal and one angle is 90°. Hence, the given parallelogram is a square.
- (vi) All the angles are equal and the adjacent sides are unequal. Hence, the given parallelogram is a rectangle.

Q14

Answer:

- (i) The given statement is false.
- The diagonals of a parallelogram bisect each other, but they are not equal in length.
- (ii) The given statement is false.
- The diagonals of a rectangle are equal and bisect each other, but they are not perpendicular.
- (iii) The given statement is false.
- All the sides of a rhombus are equal, but the diagonals are not equal.
- (iv) The given statement is true.
- (v) The given statement is false.
- Every square is a rectangle, but every rectangle is not a square.
- (vi) The given statement is true.
- (vii) The given statement is true.
- (viii) The given statement is true.
- (ix) The given statement is false.
- A rectangle is a special type of parallelogram, but every parallelogram is not a rectangle.
- (x) The given statement is true.

Parallelograms Exercise 16B

Q1

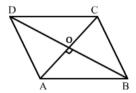
Answer:

(c) rhombus

In a rhombus, the two diagonals are not necessarily equal.

Q2

(c) 10 cm



Let ABCD be a rhombus.

Let AC and BD be the diagonals of the rhombus intersecting at a point O.

AC = 16 cm

BD = 12 cm

We know that the diagonals of a rhombus bisect each other at right angles.

$$\therefore AO = \frac{1}{2}AC$$

$$= \left(\frac{1}{2} \times 16\right) \text{ cm}$$

$$= 8 \text{ cm}$$

$$BO = \frac{1}{9} BD$$

$$=\left(\frac{1}{2}\times12\right)$$
 cm

=6 cm

From the right $\triangle AOB$:

AB² =
$$AO^2 + BO^2$$

= $\{(8)^2 + (6)^2\}$ cm²
= $(64 + 36)$ cm²
= 100 cm²
⇒ $AB = \sqrt{100}$ cm
= 10 cm

Hence, the length of the side AB is 10 cm.

Therefore, the length of each side of the rhombus is 10 cm because all the sides of a rhombus are equal.

Q3

Answer:

We know that the sum of adjacent angles of a parallelogram is 180°.

- $\Rightarrow 2x + 25 + 3x 5 = 180$
- $\Rightarrow 5x + 20 = 180$
- $\Rightarrow 5x = 180 20$
- $\Rightarrow 5x = 160$
- $\Rightarrow x = \frac{160}{5}$
- $\Rightarrow x = 32$
- Therefore, the value of x is 32.

Q4

Answer:

In a parallelogram, the diagonals do not necessarily intersect at right angles.

Q5

Answer:

(c) 70 cm

Let ABCD be a rectangle and let the diagonal AC be 25 cm, length AB be 4x cm and breadth BC be 3x cm.

Each angle of a rectangle is a right angle.

From the right $\triangle ABC$:

$$AC^2 = AB^2 + BC^2$$

$$\Rightarrow (25)^2 = (4x)^2 + (3x)^2 \Rightarrow 625 = 16x^2 + 9x^2$$

$$\Rightarrow 020 = 10x + 9x$$

$$\Rightarrow 625 = 25x^2$$

$$x^2 = \frac{625}{25} = 25$$

$$\Rightarrow x = 5$$

$$\therefore \ L \, \text{ength} \ = 4 \times 5 = 20 \ \text{cm}$$

Breadth = $3 \times 5 = 15$ cm

Q6

: Perimeter of the rectangle = 2(20+15) cm

Answer:

= 70 cm

The bisectors of any two adjacent angles of a parallelogram intersect at 90°.

07

Answer:

Let x° be the angle of the parallelogram.

Sum of the adjacent angles of a parallelogram is 180°.

$$\therefore x + \left(\frac{2}{3} \times x\right) = 180$$

$$\Rightarrow x + \frac{2x}{3} = 180$$

$$\Rightarrow \left(x + \frac{2x}{3}\right) = 180$$

$$\Rightarrow \frac{5x}{3} = 180$$

$$\Rightarrow x = \left(180 \times \frac{3}{5}\right)$$

$$\Rightarrow x = 108$$

Hence, one angle of the parallelogram is 108°.

Its adjacent angle = $(180 - 108)^{\circ} = 72^{\circ}$

Therefore, the smallest angle of the parallelogram is 72°.

08

Answer:

(a) r ectangle

In a rectangle, the diagonals do not necessarily bisect the interior angles at the vertices.

Q9

010

Answer:

(d) 8

All the sides of a square are equal.

$$AB = BC$$

$$\Rightarrow 2x + 3 = 3x - 5$$

$$\Rightarrow 3+5=3x-2x$$

Therefore, the value of x is 8.

Answer:

Let x° be the smallest angle of the parallelogram.

The sum of adjacent angles of a parallelogram is 180°.

$$x + 2x - 24 = 180$$

$$\Rightarrow 3x - 24 = 180$$

$$\Rightarrow 3x = 180 + 24$$

$$\Rightarrow 3x = 204$$
$$\Rightarrow x = \frac{204}{3}$$

$$\Rightarrow x = \frac{3}{3}$$

 $\Rightarrow x = 68$

∴ Smallest angle = 68° $L \text{ argest angle} = (180 - 68)^{\circ} = 112^{\circ}$

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