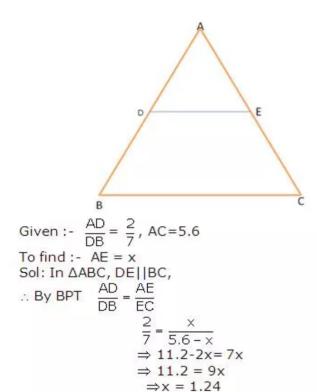
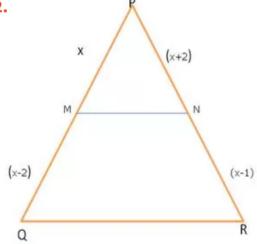
# **Chapter 15. Similarity**

# Ex 15.1

## Answer 1.

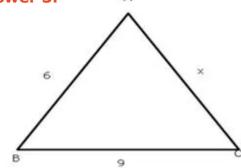


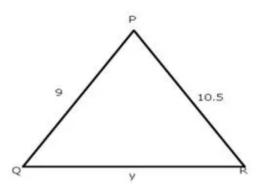
## Answer 2.



Sol: In 
$$\triangle PQR$$
,  $MN | | QR$ ,  
 $\therefore$  By BPT  $\frac{PM}{MQ} = \frac{PN}{NR}$   
 $\frac{x}{x-2} = \frac{x+2}{x-2}$   
 $\Rightarrow x^2 - x = x^2 - 4$   
 $\Rightarrow x = 4$ 

# Answer 3.





Given:- ΔABC ~ ΔPQR To find: - AC and QR Sol: AABC ~ APQR

$$\therefore \frac{AB}{PQ} = \frac{BC}{QR} = \frac{AC}{PR}$$
 (Similar sides of similar triangles)

$$\frac{6}{9} = \frac{9}{y} = \frac{x}{10.5}$$

$$\frac{6}{9} = \frac{9}{y}$$

$$\frac{6}{9} = \frac{\times}{10.5}$$

$$\Rightarrow 63 = 9x$$
$$\Rightarrow x = 7$$

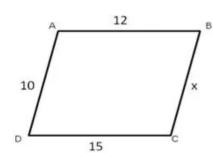
$$\Rightarrow y = \frac{81}{6}$$

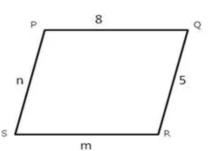
$$\Rightarrow x = 7$$

$$\Rightarrow$$
y =  $\frac{27}{2}$ 

$$\Rightarrow$$
AC = 7cm

#### Answer 4.





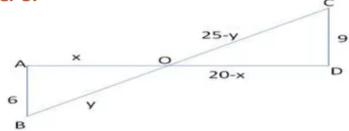
Given: quadrilateral ABCD~quadrilateral PORS

To find: x, m and n

Sol: quadrilateral ABCD~quadrilateral PORS

x = 7.5 cm, m = 10 cm, n = 6.67 cm

## Answer 5.



To find: AO, BO, CO,DO In ΔAOB and ΔCOD

 $\angle OAB = \angle ODC (90^{\circ}each)$ 

 $\angle AOB = \angle DOC$  (vertically opposite angles)

.: ΔAOB ~ΔDOC (AA corollary)

$$\therefore \frac{AO}{DO} = \frac{OB}{OC} = \frac{AB}{DC}$$

$$\frac{x}{20-x} = \frac{y}{25-y} = \frac{6}{9}$$

$$\frac{x}{20-x} = \frac{2}{3}, \frac{y}{25-y} = \frac{2}{3}$$

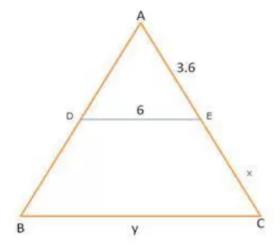
$$3x = 40 - 2x$$
,  $3y = 50 - 2y$ 

$$5x = 40, 5y = 50$$

$$x = 8, y = 10$$

$$AO = 8cm, OB = 10cm$$

# Answer 6.



Given: DE=6cm, AE=3.6cm,  $\frac{AD}{DB} = \frac{2}{3}$ , DE||BC

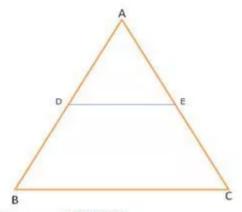
To find: BC and AC Sol: In ΔABC, DE||BC

∴By BPT 
$$\frac{AD}{DB} = \frac{AE}{EC}$$
  
 $\frac{2}{3} = \frac{3.6}{\times}$   
 $x = \frac{3.6 \times 3}{2}$   
 $= 1.8 \times 3$   
 $x = 5.4 = EC$   
∴AC = 3.6 + 5.4 = 9cm  
AC = 9cm

In  $\triangle ADE$  and  $\triangle ABC$   $\angle ADE = \angle ABC$ Similarly  $\angle AED = \angle ACB$  (corresponding angles)  $\therefore \triangle ADE \sim \triangle ABC$  (AA corollary)

$$\frac{AE}{AC} = \frac{DE}{BC}$$
 (Similar sides of angles) 
$$\frac{3.6}{9} = \frac{6}{y}$$
$$y = \frac{9 \times 6}{3.6}$$
$$y = 15$$
$$BC = 15cm$$

# Answer 7.



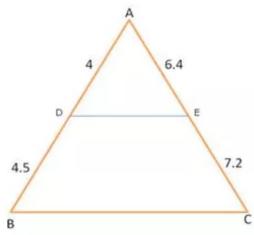
$$\frac{AD}{DB} = \frac{1.4}{4.2} = \frac{1}{3}$$
 --- (1)

$$\frac{AE}{EC} = \frac{1.8}{5.4} = \frac{1}{3}$$
 ----(2)

$$\frac{AD}{DB} = \frac{AE}{EC}$$

:.DE||BC (By converse of BPT)

#### Answer 8.

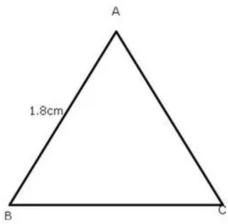


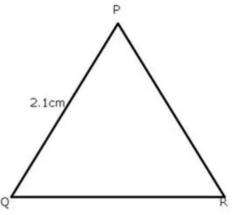
Sol: 
$$\frac{AD}{DB} = \frac{4}{4.5} = \frac{8}{9}$$
 ---- (1)  
 $\frac{AE}{EC} = \frac{6.4}{7.2} = \frac{8}{9}$  ---- (2)  
From (1) and (2)

$$\frac{AD}{DB} = \frac{AE}{EC}$$

$$\therefore DE | |BC (By converse of BPT)$$

#### Answer 9.

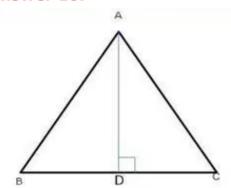


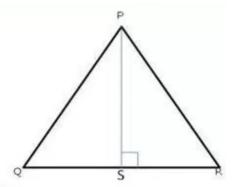


To find: 
$$\frac{Ar\Delta ABC}{Ar\Delta PQR} = \frac{AB^2}{PQ^2}$$
 The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides 
$$= \left(\frac{1.8}{2.1}\right)^2$$
 
$$= \left(\frac{6}{7}\right)^2$$
 
$$= \frac{36}{49}$$

Required ratio = 36:49

#### Answer 10.





Given: AD:PS=4:9 and ΔABC ~ ΔPQR

To find:  $\frac{Ar.\Delta ABC}{Ar.\Delta PQR}$ 

Sol:  $\frac{Ar.\Delta ABC}{Ar.\Delta PQR} = \frac{AB^2}{PQ^2}$  ----(1)

The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides

In ΔBAD and ΔQPS

 $\angle B = \angle Q (\triangle ABC \sim \triangle PQR)$  $\angle AOB = \angle PSQ (90^{\circ} each)$ 

ΔBAD ~ ΔQPS (AA corollary)

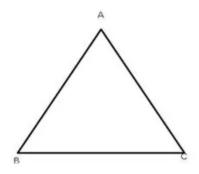
 $\therefore \frac{AB}{PQ} = \frac{AD}{PS} ----(2) \text{ (Similar sides of similar triangles)}$ 

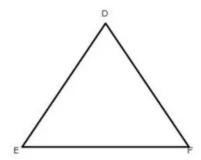
Using (1) and (2)

 $\frac{\text{Ar.}\Delta\text{ABC}}{\text{Ar.}\Delta\text{PQR}} = \frac{\text{AD}^2}{\text{PS}^2} = \left(\frac{4}{9}\right)^2 = \frac{16}{81}$ 

Required ratio is 16:81

# Answer 11.





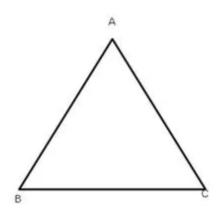
Given: ΔABC ~ΔDEF To find: Ar. of ΔDEF

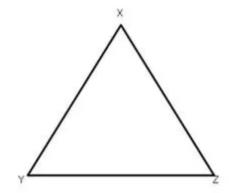
Sol: 
$$\frac{Ar.\Delta ABC}{Ar.\Delta DEF} = \frac{BC^2}{EF^2}$$

The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides

$$\frac{54}{\text{Ar.}\Delta\text{DEF}} = \left(\frac{3}{4}\right)^{2}$$
$$\frac{54}{\text{Ar.}\Delta\text{DEF}} = \frac{9}{16}$$
$$\text{Ar.}\Delta\text{DEF} = \frac{54 \times 16}{9}$$
$$= 96\text{cm}^{2}$$

#### Answer 12.





Given: ΔABC ~ ΔXYZ

To find: YZ

Sol: 
$$\frac{Ar.\Delta ABC}{Ar.\Delta XYZ} = \frac{BC^2}{YZ^2}$$
 the ra

(The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides

$$\frac{9}{16} = \frac{(2.1)^2}{YZ^2}$$

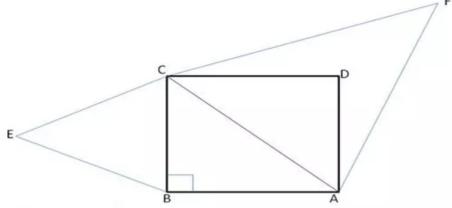
Taking square root both sides,

$$\frac{3}{4} = \frac{2.1}{YZ}$$

$$YZ = \frac{2.1 \times 4}{3}$$

$$YZ = 2.8cm$$

#### Answer 13.



In right triangle ABC,

By Pythagoras Theorem,  $AB^2 + BC^2 = AC^2$   $2 BC^2 = AC^2 ---(1) (::AB=BC)$ 

$$2 BC^2 = AC^2 --- (1) (::AB=BC$$

Given, ΔBCE ~ ΔACF

$$\frac{\text{Ar.}\Delta BCE}{\text{Ar.}\Delta ACF} = \frac{BC^2}{AC^2}$$

$$\left(\begin{array}{c} \text{The ratio of areas of two similar triangles is equal to} \\ \text{the ratio of square of their corresponding sides} \end{array}\right)$$

$$= \frac{BC^2}{AC^2}$$

$$= \frac{1}{2}$$

Required ratio is 1:2

## Answer 14.

(a) If AN : AC = 5 : 8, find  $ar(\Delta AMN)$  :  $ar(\Delta ABC)$ 

Given:  $\frac{AN}{AC} = \frac{5}{8}$ 

To Find: Ar.AARC

In AAMN and AABC

∠AMN = ∠ ACB (corresponding angles))

ZABC =ZACB

∴ △AMIN ~ △ABC (AA corollary)

 $\frac{Ar.\Delta AMN}{Ar.\Delta ABC} = \frac{AN^2}{AC^2} \left( \begin{array}{c} \text{The ratio of areas of two similar triangles is equal to} \\ \text{the ratio of square of their corresponding sides.} \end{array} \right)$ 

$$=\left(\frac{5}{8}\right)^2$$

$$\frac{Ar.\Delta AMN}{Ar.\Delta ABC} = \frac{25}{64}$$

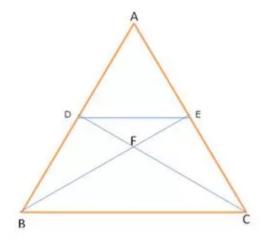
Required ratio is 25:64

(b) If 
$$\frac{AB}{AM} = \frac{9}{4}$$
, find  $\frac{Ar.(\text{trapeziumMBCN})}{Ar.(\Delta ABC)}$ 

ΔΑΜΝ ~ ΔΑΒC (proved above)

$$\therefore \frac{Ar.\Delta AMN}{Ar.\Delta ABC} = \frac{AM^2}{AB^2} = \left(\frac{4}{9}\right)^2 = \frac{16}{81}$$

#### Answer 15.



Given:  $\frac{DE}{BC} = \frac{2}{7}$ 

To find: (Similar sides of similar triangles)

In  $\triangle FDE$  and  $\triangle FCB$  $\angle FDE = \angle FCB$ 

 $\angle$ FED =  $\angle$ FBC (Alternate interior angles)

ΔFDE ~ ΔFCB (AA corollary)

 $\frac{\text{Ar.}\Delta\text{FDE}}{\text{Ar.}\Delta\text{FBC}} = \frac{\text{DE}^2}{\text{BC}^2} = \left(\frac{2}{7}\right)^2 = \frac{4}{49} \left( \frac{\text{The ratio of areas of two similar triangles is equal to}}{\text{the ratio of square of their corresponding sides}} \right)$ 

#### Answer 16.

Given:  $\frac{PT}{TR} = \frac{5}{3}$ ,

To find :  $\frac{Ar.(\Delta MTS)}{Ar.(\Delta MQR)}$ 

Sol: In ΔPST and ΔPRQ

 $\angle PST = \angle PQR$ 

 $\angle PTS = \angle PRQ$  (Corresponding angles)

: ΔPST ~ ΔPQR (AA corollary)

 $\therefore \frac{PT}{PR} = \frac{ST}{QR} = \frac{5}{8}$  (Similar sides of similar triangles)

Now, In  $\Delta$ MTS and  $\Delta$ MQR

 $\angle$ MTS =  $\angle$ MQR (Alternate interior angles)

 $\angle$ MST =  $\angle$ MRQ

.: ΔMTS ~ ΔMQR (AA corollary)

 $\therefore \quad \frac{\text{Ar.}(\Delta \text{MTS})}{\text{Ar.}(\Delta \text{MQR})} = \frac{\text{TS}^2}{\text{QR}^2} = \left(\frac{5}{8}\right)^2 = \frac{25}{64}$ 

(The ratio of areas of two similar triangles is equal to i.e. 25: 64 the ratio of square of their corresponding sides

#### Answer 17.

Given: 
$$\frac{KL}{KT} = \frac{9}{5}$$

To find: 
$$\frac{Ar.\Delta KLM}{Ar.\Delta KTP}$$

Sol: In 
$$\triangle$$
KLM and  $\triangle$ KTP  $\angle$ KLM =  $\angle$ KTP (Given)

$$\angle$$
LKM =  $\angle$ TKP(Common)

$$\therefore \frac{\text{Ar.}\Delta\text{KLM}}{\text{Ar.}\Delta\text{KTP}} = \left(\frac{\text{KL}}{\text{KT}}\right)^2 = \left(\frac{9}{5}\right)^2 = \frac{81}{25}$$

i.e., 
$$81:25$$
 (The ratio of areas of two similar triangles is equal to the ratio of square of their corresponding sides

#### Answer 18.

In 
$$\triangle$$
DEF and  $\triangle$ GHF,

$$\angle DEF = \angle GHF (90^{\circ} each)$$

$$\angle DFE = \angle GFH$$
 (Common)

ΔDEF ~ ΔGHF (AA corollary)

$$\therefore \frac{Ar.(VDEF)}{Ar.(VGHF)} = \frac{EF^2}{HF^2} ----(1)$$

(The ratio of areas of two similar triangles is equal to) the ratio of square of their corresponding sides

In right  $\triangle DEF$ , (By Pythagoras theorem)

$$DE^2 + EF^2 = DF^2$$

$$DE^{2} + EF^{2} = DF^{2}$$
  
 $EF^{2} = 10^{2} - 8^{2}$ 

$$EF^2 = 36$$

$$EF = 6$$

$$\frac{Ar.(VDEF)}{Ar.(VGHF)} = \left(\frac{6}{4}\right)^2 = \frac{9}{4}$$

# Ex 15.2

#### Answer 1.

Scale= 1:500 1cm represents 500cm 500

$$\frac{500}{100} = 5m$$

1cm represents 5m

Length of model =  $\frac{50}{5}$  = 10cm

Breadth of model =  $\frac{40}{5}$  = 8cm

Height of model =  $\frac{70}{5}$  = 14cm

## Answer 2.

20cm represents 400m

1cm represesnts  $\frac{400}{20}$  = 20cm

Width of model =  $\frac{100}{20}$  = 5cm

Length of model = 20cm

Surface area of the deck of the model= 5cm imes 20cm

 $= 100 \, \text{cm}^2$ 

#### Answer 3.

Scale: - 1:500

1cm represents 500cm

$$=\frac{500}{100} = 5m$$

1cm represents 5m

(i) Actual length of ship = 60 × 5m

= 300 m

(ii)  $1 \text{ cm}^2 \text{ represents } 5\text{m} \times 5\text{m} = 25\text{m}^2$ 

Deck area of the ship = 1500000m<sup>2</sup>

Deck area of the model =  $\frac{1500000}{25}$  cm<sup>2</sup> = 60000cm<sup>2</sup>

(iii)  $1 \text{ cm}^3 \text{ represents } 5\text{m} \times 5\text{m} \times 5\text{m} = 125 \text{ m}^3$ 

Volume of the model =  $200 \, \text{cm}^3$ 

Volume of the ship =  $200 \times 125 \,\text{m}^3$ 

 $= 25000 \,\mathrm{m}^3$ 

#### Answer 4.

15cm represents = 30m

1cm represents 
$$\frac{30}{15} = 2m$$

 $1 \text{ cm}^2$  represents  $2 \text{m} \times 2 \text{m} = 4 \text{ m}^2$ 

Surface area of the model = 150 cm<sup>2</sup>

Actual surface area of aeroplane =  $150 \times 2 \times 2 \, \text{m}^2$ 

$$= 600 \, \text{m}^2$$

50 m<sup>2</sup> is left out for windows

Area to be painted = 600 - 50

$$=50 \text{ m}^2$$

Cost of painting per  $m^2 = Rs. 120$ 

Cost of painting  $550 \text{ m}^2 = 120 \times 550$ = Rs. 66000

#### Answer 5.

1cm on map represents 12500m on land

1 cm represents 12.5km on land

Length of river on map = 54cm

Actual length of the river =  $54 \times 12.5$ 

= 675.000km

=675km

#### Answer 6.

(i) Scale: - 1: 200000

:: 1cm represents 200000cm

$$=\frac{200000}{1000\times100}$$
 =  $2km$ 

1cm represents 2km

(ii) 1cm represents 2 km

$$112^2 + 16^2$$
 represents  $2 \times 2 = 4 \text{km}^2$ 

(iii)4km² is represented by km²

$$1 \text{km}^2$$
 is represented by  $\frac{1}{4} \text{cm}^2$ 

$$20 \text{km}^2$$
 is represented by  $\frac{1}{4} \times 20 \text{cm}^2 = 5 \text{cm}^2$ 

Area on map that represents the plot of land= 5cm²

# Answer 7.

Actual area= 1872km²

Area on map represents 117 cm<sup>2</sup>

Let 1cm represents x km

 $\therefore 1 \text{cm}^2 \text{ represents } \times \times \times \text{ km}^2$ 

Actual area =  $\times \times \times \times 117 \text{ km}^2$ 

$$1872 = \times^2 \times 117$$

$$x^2 = \frac{1872}{117}$$

$$x^2 = 16$$

:: 1cm represents 4 km

Length of coastline on map = 44cm

Actual length of coastline =  $44 \times 4 \text{ km}$ 

 $= 176 \, \text{km}$ 

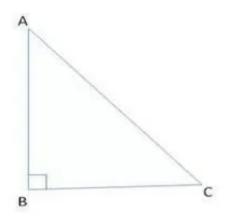
#### Answer 8.

Scale:- 1: 25000

:.1 cm represents 25000cm

$$= \frac{25000}{1000 \times 100} = 2.5 \text{km}$$

:.1cm represents 0.25km



Actual length of AB =  $6 \times 0.25$ 

 $= 1.50 \, \text{km}$ 

Area of  $\triangle ABC = \frac{1}{2} \times BC \times AB$ 

$$= \frac{1}{2} \times 8 \times 6 = 24 \text{cm}^2$$

1cm represents 0.25 km

 $1\,\text{cm}^2\,\text{represents}\,0.25\times\,0.25\text{km}^2$ 

The area of plot =  $0.25 \times 0.25 \times 24 \text{km}^2$ 

 $= .0625 \times 24$ 

 $= 1.5 km^2$ 

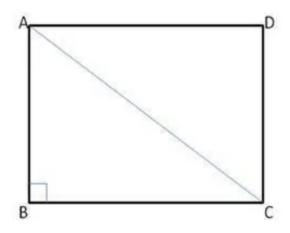
#### Answer 9.

Scale: - 1: 25000

1 cm represents 25000cm

$$= \frac{25000}{1000 \times 100} = 0.25 \text{km}$$

1 cm represents 0.25km



$$AC^2 = AB^2 + BC^2$$
  
=  $12^2 + 16^2$   
=  $144 + 256$ 

$$AC^2 = 400$$

$$AC = 20 cm$$

Actual length of diagonal =  $20 \times 0.25$ 

$$= 5.00$$

1cm represents 0.25km

 $1\text{cm}^2 \text{ represents } 0.25 \times 0.25 \text{km}^2$ 

The area of the rectangle  $ABCD = AB \times BC$ 

$$= 16 \times 12 = 192 \,\mathrm{cm}^2$$

The area of the plot =  $0.25 \times 0.25 \times 192 \text{km}^2$ 

$$= 12 km^{2}$$