## ANSWERS

## Exercise 1.1

1. (i) $\frac{5}{8}$
(ii) $\frac{9}{8}$
(iii) $\frac{509}{125}$.
2. (i) 0.25
(ii) 0.425
(iii) $2 \cdot \dot{2}$
(iv) $0.29 \dot{5} \dot{4}$
(v) $0 . \overline{571428}$
3. (i) $0 . \dot{4}$
(ii) $0 \cdot \overline{27}$
(iii) $0.3 \overline{45}$
(iv) $0 . \overline{538461}$.
4. $0 \cdot 1042$.
5. $1 \cdot 087$.
6. $-\frac{5}{7},-\frac{3}{8}, \frac{9}{14}, \frac{20}{21}$.
7. $\frac{13}{18}, \frac{7}{12},-\frac{8}{15},-\frac{17}{24}$.
8. $\frac{3}{8}, \frac{4}{11}, \frac{8}{23}, \frac{15}{46} ; 0.05$.
9. (i) Terminating decimal; 0.4375
(iii) terminating decimal; 0.544
(v) terminating decimal; 0.9
(vii) recurring decimal
(ix) recurring decimal
(ii) terminating decimal; $0 \cdot 2625$
(iv) recurring decimal
(vi) recurring decimal
(viii) terminating decimal; 1.96875
$(x)$ recurring decimal.
10. (i), (iii) and (iv).
11. (i) $\frac{4}{9}$
(ii) $\frac{1}{6}$
(iii) $\frac{5}{33}$
(iv) $\frac{368}{495}$
(v) $\frac{389}{165}$.

## Exercise 1.2

1. $\frac{43}{144} ; \frac{3}{8}, \frac{43}{144}, \frac{2}{9}$.
2. $\frac{7}{24}, \frac{13}{48} ; \frac{1}{4}, \frac{13}{48}, \frac{7}{24}, \frac{1}{3}$.
3. $-\frac{11}{24},-\frac{5}{12} ;-\frac{1}{2},-\frac{11}{24},-\frac{5}{12},-\frac{1}{3}$.
4. $\frac{27}{60}, \frac{17}{30}, \frac{41}{60} ; \frac{4}{5}, \frac{41}{60}, \frac{17}{30}, \frac{27}{60}, \frac{1}{3}$.
5. $4 \cdot 125,4 \cdot 25,4 \cdot 375$.
6. $\frac{19}{30}, \frac{2}{3}, \frac{7}{10}, \frac{11}{15}, \frac{23}{30}$.
7. $\frac{23}{30}, \frac{47}{60}, \frac{4}{5}, \frac{49}{60}$.

## Exercise 1.3

1. (i) True
(iii) False
(iv) False
(v) False.
2. (i) $\sqrt{\frac{7}{25}}, \sqrt{\frac{16}{5}}$
(ii) False
3. (i), (ii), (iii), (iv), (vi) and (viii).
4. (i) $\sqrt{15} ;-\sqrt{7}$
(ii) $\frac{9}{\sqrt{5}} ;-3 \sqrt{2}$.
5. (i) $2 \sqrt{3}, \sqrt{15},-4,3 \sqrt{2}$
(ii) $4,3 \sqrt{2}, 2 \sqrt{8}, 4 \sqrt{3}, \sqrt{50}$.
6. (i) $4 \sqrt{3}, \frac{9}{\sqrt{2}}, \frac{3}{2} \sqrt{5}, 3 \sqrt{\frac{6}{5}} \quad$ (ii) $3 \sqrt{5}, 2 \sqrt{7}, \frac{7}{3} \sqrt{2}, \frac{5}{\sqrt{3}},-\sqrt{3}$.
7. $\sqrt[3]{2}, \sqrt[6]{5}, \sqrt{3}$.
8. $\sqrt{2 \cdot 5}$.
9. $1 \cdot 5$.
10. $\sqrt{5}, \sqrt{6}$. 17. $3 \cdot 5,3 \cdot 6$.
11. $\frac{1}{\sqrt{5}}, \frac{1}{\sqrt{3}}, \frac{1}{\sqrt{2}}$.
12. $\sqrt{21}, \sqrt{22}$
13. $\sqrt{6}, \sqrt{7}, \sqrt{8}$
14. (i) $\frac{3 \sqrt{5}}{20}$
(ii) $\frac{5 \sqrt{21}}{3}$
(iii) $\frac{4+\sqrt{7}}{3}$
(iv) $3 \sqrt{2}-1$
(v) $-5-2 \sqrt{6}$
15. (i) $\frac{47+21 \sqrt{5}}{2}$
(ii) $17-12 \sqrt{2}$
(iii) $\frac{-119+31 \sqrt{14}}{7}$.
16. (i) $a=-\frac{53}{59}, b=-\frac{22}{59}$
(ii) $a=32, b=-11$. 22. $a=3, b=0$.
17. $p=0, q=1$.
18. $a=\frac{13}{7}, b=-\frac{2}{7}$.
19. 16. 
1. 98. 
1. $(i)-18$
(ii) $8 \sqrt{5}$
(iii) 322
(iv) $-144 \sqrt{5}$.

## Chapter Test

1. (i) Recurring decimal (ii) recurring decimal (iii) terminating decimal; 0.056 (iv) terminating decimal; -0.2875 (v) recurring decimal.
2. $0 \cdot 139$.
3. $23 \cdot 33$.
4. (i) $\frac{74}{55}$
(ii) $\frac{2355}{999}$.
5. $\frac{64}{117} ; \frac{7}{13}, \frac{64}{117}, \frac{5}{9}$.
6. $\frac{1}{3}, \frac{7}{24}, \frac{1}{4}, \frac{5}{24}, 0 ; \frac{3}{8}, \frac{1}{3}, \frac{7}{24}, \frac{1}{4}, \frac{5}{24}, 0,-\frac{1}{3}$.
7. (i) $2(2 \sqrt{2}-\sqrt{3})$
(ii) $\frac{57}{15}-\frac{41}{30} \sqrt{6}$
(iii) $\frac{2+\sqrt{6}-\sqrt{2}}{4}$.
8. $p=3, q=-\frac{2}{3}$.
9. (i) $550 \frac{1}{4}$
(ii) $20 \frac{7}{9}$
(iii) 970 .
10. $\frac{5}{2} \sqrt{3}, 3 \cdot 5,2 \sqrt{2}, \sqrt{10},-\frac{5}{\sqrt{2}}$.
11. $2 ; \frac{\sqrt{3}+\sqrt{5}}{2}$.
12. $\sqrt{15}, \sqrt{14}, 2 \sqrt{3} ; 3,2 \sqrt{3}, \sqrt{14}, \sqrt{15}, 4$.
13. $\sqrt{13}, \sqrt{15}, 3 \sqrt{2} ; 2 \sqrt{5}, 3 \sqrt{2}, \sqrt{15}, \sqrt{13}, 2 \sqrt{3}$.
14. $-\frac{1}{3},-\frac{1}{6}, 0, \frac{1}{6} ; \frac{1}{\sqrt{10}}$.
15. (i) $\sqrt{2} ; \sqrt{3}$ (ii) $\sqrt{2}, \sqrt{3}$.
16. Take $a=3 \sqrt{2}, b=5 \sqrt{2}$.
17. $q$ can be expressed as $q=2^{m} 5^{n}$ where $m$ and $n$ are non-negative integers.
18. (i) Rational; prime factors of $q$ are 2 or 5 or both only
(ii) rational; $q$ has a prime factor other than 2 and 5
(iii) irrational
(iv) rational; prime factors of $q$ are 2 or 5 or both only
(v) rational; $q$ has a prime factor other than 2 and 5
(vi) irrational.

## Exercise 2.1

1. ₹ $10 ; 25 \%$.
2. (i) ₹ 460
(ii) ₹ 376 .
3. $5 \%$.
4. ₹ 4000 .
5. ₹ 450 .
6. ₹ 252 .
7. Loss ₹ 15 .
8. ₹ $60 ; 33 \frac{1}{3} \%$.
9. ₹ 345 .
10. ₹ 520 .
11. $5 \frac{5}{8} \%$
12. ₹ 66 .
13. $6 \frac{1}{4} \%$.
14. ₹ $64 \cdot 80$.
15. $88 \frac{8}{9} \%$.


## Exercise 2.2

1. ₹ 66.
2. ₹ 650 .
3. $10 \%$.
4. (i) ₹ 133
(ii) ₹ 125 .
5. (i) ₹ 720 (ii) ₹ 108 (iii) $53 \%$.
6. 5 pairs.
7. (i) ₹ 240
(ii) ₹ 200 .
8. (i) ₹ 3000 (ii) ₹ 2520 (iii) $5 \%$.
9. ₹ 288.
10. ₹ 5000 .
11. ₹ 308.70 .
12. (i) ₹ 76.50
(ii) ₹ 10000
(iii) (a) ₹ 8000
(b) Loss $4 \frac{3}{8} \%$.
13. ₹ $6 ; 18.75 \%$.
14. $10 \cdot 4 \%$
15. $15 \frac{3}{8} \%$.
16. $14 \%$.
17. ₹ 36.
18. ₹ 33600 ; ₹ 33480 .
19. (i) ₹ 722 (ii) $3 \frac{1}{7} \%$.
20. X.
21. $31 \cdot 6 \%$.
22. $40 \%$.
23. ₹ 44 .
24. ₹ 2260 .
25. ₹ 300 ; ₹ 1080 ; ₹ 1100 ; ₹ 1320 .

## Chapter Test

1. ₹ 145000 .
2. 275 ml .
3. ₹ 84000 .
4. $5 \%$.
5. ₹ 230 .
6. ₹ 856 .
7. ₹ 900 .
8. ₹ 1000 .
9. ₹ 42000 .
10. ₹ 650 .
11. $29 \%$.
12. $15 \frac{15}{16} \%$.
13. (i) $14 \frac{2}{7} \%$ (ii) $25 \%$.

## Exercise 3.1

1. ₹ 11236 ; ₹ 1236 .
2. (i) ₹ 1000
(ii) ₹ 13500
(iii) ₹ 1080 (iv) ₹ 14580
(v) ₹ 2080 .
3. (i) ₹ 16500
(ii) ₹ 1650
(iii) ₹ 19965.
4. ₹ 1540 ; ₹ 18634 .
5. (i) ₹ 3750
(ii) ₹ 54675
(iii) ₹ 4374
(iv) ₹ 59049.
6. ₹ $70246 \cdot 40$.
7. (i) ₹ 17600
(ii) ₹ 19360 (iii) ₹ 3360
(iv) ₹ 1760 (v) ₹ 21296.
8. ₹ 787 .
9. ₹ 46305 ; ₹ 6305 .
10. ₹ 17658 ; ₹ 2658.
11. ₹ 27104 ; ₹ 7104.
12. (i) $10 \%$ (ii) ₹ 14520
(iii) ₹ 2520 .
13. (i) $8 \%$
(ii) ₹ 1350
(iii) ₹ 19683
(iv) ₹ 1458
(v) ₹ 4058 .
14. ₹ 26620 ; ₹ 6620 .

## Exercise 3.2

1. ₹ $9331 \cdot 20$; ₹ $1331 \cdot 20$.
2. ₹ $13867 \cdot 50 ; 1867 \cdot 50$.
3. ₹ $70246 \cdot 40$; ₹ $20246 \cdot 40$.
4. ₹ 22781 ; ₹ 6781 .
5. ₹ $36602 \cdot 50$; ₹ $11602 \cdot 50$.
6. ₹ 4056 ; ₹ 306 .
7. ₹ 9261 ; ₹ 1261.
8. ₹ 32.

## Chapter Test

1. (i) ₹ 1650
(ii) ₹ 16650
(iii) ₹ 1831.50
(iv) ₹ 18481.50
(v) ₹ $3481 \cdot 50$.
2. (i) ₹ 15400
(ii) ₹ 1540
(iii) ₹ 18634
(iv) ₹ 4634
(v) ₹ 1694.
3. (i) $8 \%$
(ii) ₹ 864
(iii) ₹ 12597.
4. ₹ 18522 ; ₹ 2522.
5. ₹ $31492 \cdot 80$; ₹ $6492 \cdot 80$.
6. ₹ 72 .
7. ₹ $42182 \cdot 40$; ₹ $4682 \cdot 40$.

## Exercise 4.1

1. (i) $4 x^{2}+28 x y+49 y^{2}$
(ii) $\frac{1}{4} x^{2}+\frac{2}{3} x y+\frac{4}{9} y^{2}$.
2. (i) $9 x^{2}+\frac{1}{4 x^{2}}+3$
(ii) $9 x^{4} y^{2}+30 x^{2} y z+25 z^{2}$.
3. (i) $9 x^{2}+\frac{1}{4 x^{2}}-3$
(ii) $\frac{1}{4} x^{2}-\frac{3}{2} x y+\frac{9}{4} y^{2}$.
4. (i) $x^{2}+8 x+15$
(ii) $x^{2}-2 x-15$
(iii) $x^{2}+2 x-63$
(iv) $x^{2}-5 x y+6 y^{2}$.
5. (i) $x^{2}+4 y^{2}+z^{2}-4 x y+4 y z-2 z x$
(ii) $4 x^{2}+9 y^{2}+16 z^{2}-12 x y-24 y z+16 z x$.
6. (i) $4 x^{2}+\frac{9}{x^{2}}+13-\frac{6}{x}-4 x$
(ii) $\frac{4}{9} x^{2}+\frac{9}{4 x^{2}}-1-\frac{4}{3} x+\frac{3}{x}$.
7. (i) $x^{3}+6 x^{2}+12 x+8$
(ii) $8 a^{3}+b^{3}+12 a^{2} b+6 a b^{2}$.
8. (i) $27 x^{3}+\frac{1}{x^{3}}+27 x+\frac{9}{x}$
(ii) $8 x^{3}-12 x^{2}+6 x-1$.
9. (i) $125 x^{3}-27 y^{3}-225 x^{2} y+135 x y^{2}$
(ii) $8 x^{3}-\frac{1}{27 y^{3}}-\frac{4 x^{2}}{y}+\frac{2 x}{3 y^{2}}$.
10. (i) $2\left(a^{2}+b^{2}\right)$
(ii) $4 a b$.
11. (i) $2\left(a^{2}+\frac{1}{a^{2}}\right)$
(ii) 4 .
12. (i) $3-3 x$
(ii) 0 .
13. (i) $49 p^{2}-81 q^{2}$
(ii) $4 x^{2}-\frac{9}{x^{2}}$.
14. (i) $4 x^{2}-4 x y+y^{2}-9$
(ii) $9 x^{2}-30 x+25-y^{2}$.
15. (i) $x^{2}-6 x+9-\frac{4}{x^{2}}$
(ii) $625-16 x^{4}$.
16. (i) $x^{2}+4 x y+4 y^{2}+10 x+20 y+21$
(ii) $4 x^{2}+4 x y+y^{2}-8 x-4 y-45$
(iii) $x^{2}-4 x y+4 y^{2}-2 x+4 y-15$
(iv) $9 x^{2}-24 x y+16 y^{2}-24 x+32 y+12$.
17. (i) $8 p^{3}+27 q^{3}$
(ii) $x^{3}+\frac{1}{x^{3}}$.
18. (i) $27 p^{3}-64 q^{3}$
(ii) $x^{3}-\frac{27}{x^{3}}$.
19. $8 x^{3}+27 y^{3}+64 z^{3}-72 x y z$.
20. (i) $x^{3}+6 x^{2}+11 x+6$
(ii) $x^{3}-x^{2}-14 x+24$.
21. 0 ; -37 .
22. 4. 
1. (i) 10201
(ii) 1006009
(iii) $104 \cdot 04$.
2. (i) 9801
(ii) 994009
(iii) 96.04 .
3. (i) 1092727
(ii) 970299
(iii) $1030 \cdot 301$.
4. 0 .
5. (i) 13770
(ii) -16380 .
6. 7. 

## Exercise 4.2

1. 74. 
1. 116. 
1. 25. 
1. 352. 
1. 68. 
1. (i) $\pm 5$
$(i i) \pm 1$.
2. $(i) \pm 8$
(ii) $\pm 32$.
3. (i) $\pm 15$
(ii) $\pm 135$.
4. (i) 26 (ii) 5 .
5. 11. 
1. (i) $\pm 7$ (ii) $169 \frac{1}{2}$ (iii) $310 \frac{1}{2}$ or $254 \frac{1}{2}$. 12. 123 .
2. 63. 
1. 135. 
1. (i) 14
(ii) 194
(iii) 52
(iv) $\pm 2 \sqrt{3}$.
2. 727. 
1. (i) 7
(ii) $\pm 3$
(iii) $\pm 18$.
2. (i) $\pm 4 \sqrt{2}$ (ii) $\pm 24 \sqrt{2}$.
3. 45
4. $\pm 5$.
5. $\pm 445$.
6. $\pm 3$.
7. $\pm 22 \frac{1}{2}$.
8. (i) 7 (ii) 18.
9. (i) 5 (ii) $\pm \sqrt{29}$ (iii) $\pm 5 \sqrt{29}$.
10. 0. 
1. $2 \sqrt{3}$. $\quad 31.100$.
2. 22. 
1. $\pm 15$. 34. -2 .
2. 721. 
1. 10 .
2. 152. 

## Chapter Test

1. (i) $4 x^{2}+9 y^{2}+12 x y-25$
(ii) $36+16 a^{2}+49 b^{2}-48 a+56 a b-84 b$
(iii) $343-27 x^{3} y^{3}-441 x y+189 x^{2} y^{2}$
(iv) $x^{3}+y^{3}+3 x^{2} y+3 x y^{2}+6 x^{2}+6 y^{2}+12 x y+12 x+12 y+8$
2. $x^{8}-256$.
3. 999996 .
4. 0 .
5. 27. 
1. $p^{2}-q^{2}=4$.
2. 104. 
1. (i) 4
(ii) 52
(iii) 2702.
2. $27+19 \sqrt{2} .11 . \pm 26 \frac{26}{27}$.
3. $-30 \sqrt{3}$
4. 85. 
1. (i) -10 (ii) 29 .
2. 6. 

## Exercise 5.1

1. (i) $4 x y^{2}(2 y+3 x)$
(ii) $3 a x^{2}(5 x-3)$ :
2. (i) $7 p y(3 y-8)$
(ii) $2 x^{2}(2 x-3)$.
3. (i) $2 \pi r(r-2)$
(ii) $2(9 m+8 n)$.
4. (i) $5 a b c(5 c-3 a b)$
(ii) $14 p q^{2} r(2 p-3 r)$.
5. (i) $2 x\left(4 x^{2}-3 x+5\right)$
(ii) $2(7 m n+11 m-31 p)$.
6. (i) $6 p q(3 p q-4 q+5 p)$
(ii) $3 a^{2} b^{2}(9 a b-6 b+25 a)$.
7. (i) $5(2 p-3 q)(3 a-2 b)$
(ii) $3\left(x^{2}+y^{2}\right)(a+2 b)$.
8. (i) $2(x+2 y)^{2}(3 x+6 y+4)$
(ii) $7(a-3 b)\left[2(a-3 b)^{2}-3 p\right]$.
9. (i) $5(2 p+q)\left[2 a(2 p+q)^{2}-3 b(2 p+q)+7\right]$
(ii) $\left(x^{2}+y^{2}-z^{2}\right)(x-y-z)$.

## Exercise 5.2

1. (i) $(x+y)(x-1)$
2. (i) $(x-y)(5 y-7)$
3. (i) $(a-b)(a b+3)$
4. (i) $(2 y-1)(3 x y-5)$
5. (i) $(1-a)(1-b)$
6. (i) $(x+y)\left(x+y^{2}\right)$
7. (i) $(b+1)(a b-1)$
8. (i) $(5+2 r)(p h-2 q k)$
9. (i) $(b x-a y)(a x-b y)$
(ii) $(y-z)(y-5)$.
(ii) $(5 p-8 q)(p-2)$.
(ii) $(x-3)\left(x^{2}+1\right)$.
(ii) $(x-2 y)(3 a+4 b)$.
(ii) $(a-2 b)(a-c)$.
(ii) $(y-x)\left(y+x^{2}\right)$.
(ii) $(a-2 b)(2-x)$.
(ii) $(x-a)(x-2 b)$.
(ii) $\left(x^{2}+y^{2}\right)\left(a^{2}+b^{2}\right)$.
10. (i) $(a-2 b)\left(a^{2}+b\right)$
(ii) $3(x-1)(x y+4)$.
11. $(a+b)(a b-b c+x y)$.
12. $(a-b)\left(x^{2}+y^{2}+z^{2}\right)$.

## Exercise 5.3

1. (i) $(2 x+5 y)(2 x-5 y)$
(ii) $(3 x+1)(3 x-1)$.
2. (i) $6(5+a)(5-a)$
(ii) $2(4 x+3 y)(4 x-3 y)$.
3. (i) $(x-y+3)(x-y-3)$
(ii) $(4 x+3 y)(2 x+3 y)$.
4. (i) $5(2 x+3 y)(2 x-3 y)$
(ii) $-(7 x+2 y)(x+2 y)$.
5. (i) $2(x+3 y)(x-7 y)$
(ii) $2 x(8-x)$.
6. (i) $3(6 a+b-c)(6 a-b+c)$
(ii) $\pi a\left(a^{2}+\pi b\right)\left(a^{2}-\pi b\right)$.
7. (i) $8(2 x+1)(3 x-1)$
(ii) $(x+1)(x-1)$.
8. (i) $(x-2 y)(1-x-2 y)$
(ii) $(2 a+b)(2 a-b+1)$.
9. (i) $(a-b)(a+b-2)$
(ii) $(a-b)(a+b-1)$.
10. (i) $(3+x-y)(3-x+y)$
(ii) $\left(3 x^{2}+x+1\right)\left(3 x^{2}-x-1\right)$
11. (i) $\left(3 x^{2}+x+6\right)\left(3 x^{2}-x-6\right)$
(ii) $(x+1)(x-1)(x-5)$.
12. (i) $\left(a^{2}+b^{2}-1\right)\left(a^{2}-b^{2}+1\right)$
(ii) $x(x+5)(x-5)$.
13. (i) $2\left(x^{2}+4\right)(x+2)(x-2)$
(ii) $(b+c)(a+b+c)(a-b-c)$.
14. (i) $(a+b)(a+b+1)(a+b-1)$
(ii) $(x-y+a+b)(x-y-a-b)$.
15. (i) $(a c-b d+b c+a d)(a c-b d-b c-a d)$
(ii) $(x-y)(4 x+y+2)$.
16. (i) $\left(x-\frac{1}{x}+3\right)\left(x-\frac{1}{x}-3\right)$
(ii) $\left(x^{2}+x+3\right)\left(x^{2}-x+3\right)$.
17. (i) $\left(a^{2}+b^{2}+3 a b\right)\left(a^{2}+b^{2}-3 a b\right)$
(ii) $\left(x^{2}+4 x+1\right)\left(x^{2}-4 x+1\right)$
18. (i) $\left(x^{2}+7\right)^{2}-(5 x)^{2}$
$\begin{array}{ll}\text { (ii) }\left(x^{2}-5 x\right)^{2}-7^{2} & \text { (iii) } x^{2}-(5 x-7)^{2}\end{array}$
19. (i) 958000
(ii) 9980 .
20. (i) $\frac{97}{36}$
(ii) $\frac{13}{6}$
(iii) $\frac{793}{216}$
(iv) $\frac{6305}{1296}$.
21. (i) 0 (ii) 0 .

## Exercise 5.4

1. (i) $(x+2)(x+3)$
2. (i) $(x+7)(x-1)$
3. (i) $(y-9)(y+2)$
4. (i) $(x-2)(2 x-3)$
5. (i) $(2 x+5)(3 x-2)$
6. (i) $(x-2)(2 x+3)$
7. (i) $(y+5)(2 y-9)$
8. (i) $(4 x+5)(3 x-2)$
9. (i) $10(2 x-3)(3 x+1)$
10. (i) $(x+8 y)(2 x-3 y)$
11. (i) $(x+4 y)(5 x-3 y)$
12. (i) $(a b-6)(2 a b+5)$
13. (i) $(x-y-5)(x-y-1)$
14. (i) $(2 a-5)(2 a-1)$
15. (i) $(1-3 a-3 b)(3+4 a+4 b)$
16. (i) $(x+y+4)(x-6 y+4)$
17. $(3 a-4)(a-5)$.
(ii) $(x-1)(x-7)$.
(ii) $(y+9)(y-2)$.
(ii) $(a+6)(a-9)$.
(ii) $(3 x-1)(2 x+5)$.
(ii) $(3 x+1)(2 x-3)$.
(ii) $(x+1)(3 x-7)$.
(ii) $(1-2 x)(5+6 x)$.
(ii) $(x-8)(x-2)$.
(ii) $(x+y)(x-7 y)$.
(ii) $(2 x-3 y)(3 x+2 y)$.
(ii) $(x y+4)(x y-12)$.
(ii) $(2 a+b)(a-b)$.
(ii) $(2 x-y-7)(2 x-y-4)$.
(ii) $(1-3 a-3 b)(1+a+b)$.
(ii) $\left(a^{2}-10\right)(a+1)(a-1)$.
(ii) $(x+2)(x-4)(x+3)(x-5)$.
18. $(x-1)(2 x+7)(x+4)(2 x-3)$.

## Exercise 5.5

1. (i) $(2 x+y)\left(4 x^{2}-2 x y+y^{2}\right)$
(ii) $(4 x-5 y)\left(16 x^{2}+20 x y+25 y^{2}\right)$.
2. (i) $(4 x+1)\left(16 x^{2}-4 x+1\right)$
(ii) $7(a+2 b)\left(a^{2}-2 a b+4 b^{2}\right)$.
3. (i) $\left(\frac{x^{2}}{7}+\frac{7}{x^{2}}\right)\left(\frac{x^{4}}{49}-1+\frac{49}{x^{4}}\right)$
(ii) $\left(2 x-\frac{1}{3 y}\right)\left(4 x^{2}+\frac{2 x}{3 y}+\frac{1}{9 y^{2}}\right)$.
4. (i) $x^{2}(1+x)\left(1-x+x^{2}\right)$
(ii) $4 x(2 x-5)\left(4 x^{2}+10 x+25\right)$.
5. (i) $(3 x y-2)\left(9 x^{2} y^{2}+6 x y+4\right)$
(ii) $(7 x+y)\left(13 x^{2}-4 x y+19 y^{2}\right)$.
6. (i) $(a+b)\left(a^{2}-a b+b^{2}+1\right)$
(ii) $(a-b)\left(a^{2}+a b+b^{2}-1\right)$.
7. (i) $(x+1)\left(x^{2}-x+2\right)$
(ii) $(a-5)\left(a^{2}+5 a+24\right)$.
8. (i) $(x+4)\left(x^{2}+2 x+4\right)$
(ii) $(a-2 b)\left(a^{2}-a b+b^{2}\right)$.
9. (i) $(a+2 b)\left(2 a^{2}-4 a b+8 b^{2}-5\right)$
(ii) $\left(a-\frac{1}{a}\right)\left(a^{2}+\frac{1}{a^{2}}-1\right)$.
10. (i) $(a+b)(a-b)\left(a^{2}+a b+b^{2}\right)\left(a^{2}-a b+b^{2}\right)$
(ii) $(x+1)(x-1)\left(x^{2}+x+1\right)\left(x^{2}-x+1\right)$.
11. (i) $(2 x+3 y)(2 x-3 y)\left(4 x^{2}+6 x y+9 y^{2}\right)\left(4 x^{2}-6 x y+9 y^{2}\right)$
(ii) $\frac{1}{x}(x-2)\left(x^{2}+2 x+4\right)$
12. (i) $2(5 a-5 b+1)\left(25 a^{2}-50 a b+25 b^{2}-5 a+5 b+1\right)$
(ii) $(2 a+b)(2 a-b)(2 x-y)\left(4 x^{2}+2 x y+y^{2}\right)$.
13. (i) $(x+y)\left(x^{2}-x y+y^{2}\right)\left(x^{6}-x^{3} y^{3}+y^{6}\right)$
(ii) $(x-2)\left(x^{2}+2 x+4\right)(x+1)\left(x^{2}-x+1\right)$

## Chapter Test

1. (i) $5(2 x-3)\left[3(2 x-3)^{2}-2\right]$
(ii) $(b-c)[a(b+c)+d]$.
2. (i) $(x+1)\left(2 a^{2}-b\right)$
(ii) $(p-a)(p-2 b)$.
3. (i) $(x-z)\left(x z+y^{2}\right)$
(ii) $5 a(a-1)\left(a^{2}+6\right)$.
4. (i) $(c-d)(b c-b d-a+3)$
(ii) $(x-1)\left(x^{2}-y+1\right)$.
5. (i) $(x-y)(x+y+z)$
(ii) $a^{4} x^{4}\left(a^{4}+x^{4}\right)\left(a^{2}+x^{2}\right)(a+x)(a-x)$.
6. (i) $(3 x+2+4 y)(3 x+2-4 y)$
(ii) $\left(x^{2}+x+2\right)\left(x^{2}-x+2\right)$.
7. (i) $(3 x-5 y)(7 x-8 y)$
(ii) $4 x y(x-4)(x-7)$.
8. (i) $(x y-9)(x y+8)$
(ii) $x y(x+4 y)(9 x+5 y)$.
9. (i) $(3 a-2 b+5)(3 a-2 b-2)$
(ii) $\left(x^{2}-3 x+5\right)(x-1)(x-2)$.
10. (i) $(x+1)(x-2)\left(4 x^{2}-4 x+3\right)$
(ii) $\left(x^{2}+9 y^{2}+3 x y\right)\left(x^{2}+9 y^{2}-3 x y\right)$.
11. (i) $\left(\frac{2}{3} x-\frac{1}{2} y\right)\left(\frac{4}{9} x^{2}+\frac{1}{3} x y+\frac{1}{4} y^{2}\right)$
(ii) $(x+4)\left(x^{2}-4 x+16\right)(x-1)\left(x^{2}+x+1\right)$.
12. (i) $\left(x+\frac{1}{x}\right)\left(x^{2}-1+\frac{1}{x^{2}}+x-\frac{1}{x}\right) \quad$ (ii) $4 x\left(x^{2}+3\right)\left(3 x^{2}+1\right) . \quad 14.931$.

## Exercise 6.1

1. (i) $s=\frac{v^{2}-u^{2}}{2 a}$. (ii) $a=\frac{2(s-u t)}{t^{2}}$.
2. (i) $\mathrm{R}= \pm \sqrt{\frac{\mathrm{A}}{\pi}+r^{2}}$
(ii) $x= \pm \sqrt{\frac{2(\mathrm{~W}-p q)}{\mathrm{N}}}$.
3. (i) $h=\frac{\mathrm{S}-2 \pi r^{2}}{2 \pi r}$
(ii) $m=\frac{n \mathrm{P}}{1-\mathrm{P}}$.
4. (i) $x=\frac{b(t+1)}{a-t}$
(ii) $r_{1}=\frac{\mathrm{R} r_{2}}{r_{2}-\mathrm{R}}$.
5. (i) $\mathrm{I}=\frac{\mathrm{T}^{2} \mathrm{MH}}{4 \pi^{2}} \quad$ (ii) $t= \pm \sqrt{\frac{1-c}{1+c}}$.
6. (i) $n= \pm \sqrt{\frac{l \mathrm{R} m^{2}}{\mathrm{R} l-m^{2}}}$ (ii) $c=-a x^{2}-b x$.
7. $p=\frac{2(q+4 r)}{5}$.
8. $n=\frac{l-a+d}{d}$.
9. $m=\frac{b-d p}{c p-a}$.
10. $n=\frac{3 x}{t x+y}$.
11. $x=\frac{3}{2}(a+b)$.
12. $z=\frac{2(x+4)}{11 x-6}$

## Exercise 6.2

1. $x=\frac{3 y+1}{2-y} ; 4$.
2. $\mathrm{H}=2(\mathrm{~W}+20) ; 180$.
3. $h=\frac{\mathrm{A}}{2 \pi r}-r ; 9$.
4. $c=\frac{\mathrm{T}}{n} ; \operatorname{Rs} 1 \cdot 50$.
5. $c=\frac{a-b}{b t}, 0.001$.
6. $r=\frac{q}{p q-1} ; 1 \frac{1}{20}$.
7. $u=v-a\left(t_{2}-t_{1}\right) ; 7$.
8. 5. 
1. $a= \pm \sqrt{2 b\left(\frac{p+q}{p-q}\right)} ; \pm 6$.
2. $v=\frac{u f}{u-f} ; 10.5$.
3. $d=\frac{2(s-u n)}{n(n-1)} ;-1$
4. $c=\frac{100(y-x)}{y+x} ; 50$.
5. $d=n-3$; (i) 7 (ii) 8 .

## Chapter Test

1. (i) $\mathrm{T}=2 \pi \sqrt{\frac{l}{g}}$
(ii) $l=\frac{T^{2} g}{4 \pi^{2}}$
(iii) $\frac{44}{35} \mathrm{sec}$.
2. $x= \pm \sqrt{\frac{a+b}{c}} ; \pm \sqrt{2}$.
3. $x=\frac{y+3}{y-1} ;-1,3$.
4. $x=\frac{a-y}{k-y} ; 2$.
5. $z=\frac{x}{2} ; \frac{5}{2}$.

## Exercise 7

1. (i) 18
(ii) $3-2 \sqrt{2}$.
2. (i) $\frac{10}{9}$
(ii) 4.
3. (i) -25 (ii) $6 \frac{1}{2}$.
4. $(i)-1$
(ii) 10 .
5. (i) 1
(ii) $\frac{13}{4}$.
6. (i) $\frac{25}{12}$ (ii) 7 .
7. (i) $2 \frac{1}{12}$
(ii) 7.
8. (i) -1
(ii) -2 .
9. $(i)-\frac{1}{2}$
(ii) $2 \frac{1}{4}$.
10. 11. 
1. $78 \frac{1}{2}$.
2. $x=6, p=\frac{5}{6}$.
3. $x=-6, a=2$.
4. $x=-1, y=\frac{2}{3}$. 15. 10 .
5. -7 .
6. 30. 
1. 4. 
1. 0 .
2. 6 cm .

## Chapter Test

1. 5. 
1. $\frac{1}{2}$.
2. 2. 
1. 1 .
2. 2 .
3. $\frac{5+3 \sqrt{5}}{10}$.
4. $1 \frac{3}{5}$.
5. 1 .
6. $-\frac{14}{13}$.
7. -104 .
8. 8. 
1. 4 cm .

## Exercise 8.1

1. (i) $x=1, y=4 \quad$ (ii) $x=-8, y=-4$. $\quad$ 2. (i) $a=2, b=1 \quad$ (ii) $x=2, y=-\frac{3}{2}$.
2. (i) $x=3, y=4$
(ii) $x=7 \frac{27}{31}, y=2 \frac{13}{31}$.
3. (i) $x=4, y=3$ (ii) $x=\frac{21}{20}, y=-\frac{3}{10}$.
4. (i) $x=5, y=-3$ (ii) $x=2, y=1$.
5. (i) $x=12, y=8$ (ii) $x=\frac{26}{11}, y=-\frac{5}{11}$.
6. (i) $x=\frac{26}{3}, y=-\frac{8}{3}$ (ii) $x=\frac{3}{4}, y=-\frac{9}{4}$.
7. (i) $x=5, y=2$ (ii) $x=3, y=2$.
8. (i) $x=4, y=-4$ (ii) $x=2, y=-1$.
9. (i) $x=\frac{1}{5}, y=-2$ (ii) $x=2, y=1$
10. (i) $x=4, y=-2$ (ii) $x=\frac{1}{2}, y=\frac{1}{3}$.
11. (i) $x=0, y=0 ; x=7, y=1$
(ii) $x=0, y=0 ; x=\frac{11}{7}, y=\frac{11}{3}$.
12. (i) $x=4, y=5 \quad$ (ii) $x=2, y=1$.
13. $x=15, y=5 ; 3$.
14. (i) $x=2, y=1$ (ii) $x=\frac{1}{2}, y=\frac{5}{4}$.
15. $x=\frac{16}{5}, y=\frac{23}{5} ; p=\frac{19}{8}$.
16. $x=7, y=9 ; x-3 y=-20,5 y-2 x=31$.
17. $a=2, b=3$.
18. 28 cm .
19. Yes; $x=7, y=2$.

## Exercise 8.2

3. 15 sq. units.
4. 6 sq. units.
5. (i) -7 (ii) 3 .
6. 2. 
1. $a=0, b=1$.

## Exercise 8.3

1. $x=-2, y=-5$.
2. $x=-4, y=-2$.
3. $x=2, y=-2$.
4. $x=-1, y=0$.
5. $x=2, y=2$.
6. $x=2, y=1$.
7. (ii) $(-2,-1)$
(iii) $4 \cdot 5 \mathrm{~cm}$.
8. $x=2, y=-1$.
9. (ii) $(2,4) ; 6 \frac{2}{3}$ sq. units.
10. $x=1, y=-2 ; \quad \frac{3}{2}$ sq. units.
11. $x=2, y=1 ; \frac{4}{3}$ sq. units.
12. $(-3,2),(-3,6),(3,2)$.
13. $(0,0),(5,0),(2,2)$; 5 sq. units.

## Chapter Test

1. (i) $x=3, y=4 \quad$ (ii) $x=14, y=2$.
2. (i) $x=-2, y=7$
(ii) $x=3 \cdot 2, y=2 \cdot 3$.
3. (i) $x=0, y=0 ; x=\frac{1}{3}, y=\frac{1}{4}$
(ii) $x=8, y=3$.
4. (i) $x=1, y=-1$
(ii) $x=2, y=3$.
5. $x=3, y=-1 ; k=2$.
6. $x=3, y=2 ; 14$.
7. Yes; $x=\frac{1}{3}, y=\frac{1}{2}$.
8. 12 cm .
9. $x=5, y=1$.
10. $x=2, y=-1$.
11. $(4,5) ; 12.5$ sq. units.
12. $(-3,-2),(5,1)$ and $(1,6) . \quad$ 13. $(2,-1),(3,2),(-4,2) ; 10 \cdot 5$ sq. units.

## Exercise 9.1

1. 33. 
1. -7 .
2. 7. 
1. 4. 
1. 15,10 .
2. Dress ₹ 480 , belt ₹ 90 .
3. Don 765, Peter 660.
4. $6 \frac{1}{4}$.
5. 60 cm .
6. 19. 
1. 64. 
1. 88. 
1. 37,39 . 14. $3,5,7$.
2. $22,24$.
3. 45 years, 20 years.
4. 40 years, 20 years.
5. Anand 14 years, Anju 9 years, father 34 years.
6. 18 years, 8 years.
7. ₹ 9900 .
8. ₹ 90000 , ₹ 120000 .
9. 73. 
1. $26,27,28$.
2. 73. 
1. 78. 
1. 71 .
2. 83. 
1. 96 square units.
2. $25 \mathrm{~m}, 20 \mathrm{~m}$.
3. 4 m .
4. 12 litres. 32.80 ml .
5. Single-bed room ₹ 840 , double-bed room ₹ 1260 .
6. Shirt ₹ 360 , tie ₹ 156 .
7. 23,9 . 38.0 .6 km .
8. $25 \mathrm{~km} / \mathrm{hr}, 30 \mathrm{~km} / \mathrm{hr}$.
9. $\frac{1}{30}+\frac{1}{x}=\frac{1}{20} ; 60$
10. $\frac{15}{29}$.
11. 3 km .
12. $37.5 \mathrm{~km} / \mathrm{hr}$.
13. $540 \mathrm{~km} / \mathrm{hr}, 580 \mathrm{~km} / \mathrm{hr}$.
14. $3 \mathrm{~km} / \mathrm{hr}$.
15. 10 kg .

## Exercise 9.2

1. $33,17$.
2. $11,-9$.
3. 33,10 .
4. ₹ 206.
5. 16 kg and 20 kg .
6. 10,8 .
7. 20 paise 20 coins, 25 paise 18 coins.
8. 20 rupee notes $=16,5$ rupee notes $=12$.
9. 8 and 12 .
10. $\frac{2}{15}$.
11. $\frac{8}{15}$.
12. $\frac{6}{8}$.
13. 43. 
1. 34. 
1. 72. 
1. 84 .
2. 45. 
1. 842 .
2. 34 years, 14 years.
3. ₹ 800 . 21. ₹ 5000 at $12 \%$ and ₹ 7000 at $10 \%$.
4. Table ₹ 600 ; chair ₹ 400 .
5. A has ₹ 500 , B has ₹ 900 .
6. 60. 
1. 4 litres $25 \%, 6$ litres $50 \%$.
2. 80 gm 18 -carat, 40 gm 12 -carat. 27. A in 25 days, $B$ in $37 \frac{1}{2}$ days.
3. 18 days.
4. 20 hours, 30 hours.
5. $10 \mathrm{~km} / \mathrm{hr}, 40 \mathrm{~km} / \mathrm{hr}$.
6. 360 km .
7. $15 \mathrm{~km} / \mathrm{hr}, 5 \mathrm{~km} / \mathrm{hr}$.
8. $8 \mathrm{~km} / \mathrm{hr}, 3 \mathrm{~km} / \mathrm{hr}$.
9. $520 \mathrm{~km} / \mathrm{hr}, 40 \mathrm{~km} / \mathrm{hr}$.
10. ₹ 1200 , ₹ 70 .

## Chapter Test

1. 12. 
1. 3 weeks 5 days.
2. 660. 
1. 10. 
1. 84 years.
2. Rohan 13 years, his sister 5 years.
3. $1325 \mathrm{~m}^{2}$.
4. ₹ 1000 , ₹ 700 , ₹ 500 .
5. ₹ 78 .
6. 150. 
1. Almonds 400 gm , cashew kernel 300 gm .
2. 8. 
1. $₹ 8$ per regular hour and $₹ 10$ per hour for overtime.
2. 16. 
1. Man's age 42 years, his son's age 12 years.
2. $113 \mathrm{~m}^{2}$.
3. 40 metres.
4. 19.5 metres.
5. Longer candle 27 cm , smaller candle 24 cm .

## Exercise 10

1. (i) $a^{5} b^{10}$
(ii) $\frac{1}{16 x^{2} y^{2}}$.
2. (i) $8 a^{-9} b^{6}$
(ii) $a+b$.
3. (i) $\frac{1}{x+y}$
(ii) $3 \times(10)^{-8}$.
4. (i) $5 a b$
(ii) $2 \frac{1}{4}$.
5. (i) $2 \frac{1}{2}$
(ii) 0.3 .
6. (i) 9
(ii) $1 \frac{11}{16}$.
7. (i) $3^{3 n}$
(ii) $\frac{1}{6}$.
8. (i) $\frac{1}{2}$
(ii) $-12 \frac{3}{4}$.
9. (i) $\frac{1}{27}$
(ii) $2 x$.
10. (i) 19
(ii) 231 .
11. (i) 12
(ii) 27 .
12. (i) $2 \frac{1}{4}$
(ii) 19 .
13. (i) $\frac{1}{2}$
(ii) 243 .
14. (i) -2
(ii) $\frac{4}{21}$.
15. (i) 4
(ii) $\frac{1}{25}$.
16. (i) -42
(ii) 98.25 .
17. (i) 3
(ii) $x-\frac{1}{x}$.
18. (i) 1
(ii) 1 .
19. (i) 1
(ii) 1
(iii) $x^{2\left(a^{3}+b^{3}+c^{3}\right)}$
20. (i) $\frac{a b}{b-a}$
(ii) 1 .
21. $1, \frac{1}{x^{2} y^{2}}, 9 a^{6}$.
22. (i) $27 \frac{1}{4} \quad$ (ii) $-7 \frac{8}{9}$.
23. 3. 
1. 6. 
1. $x=2, y=3, z=7$.
2. $x=2, y=-\frac{2}{3}$.
3. 6. 
1. (i) $-\frac{3}{2}$
(ii) 4
(iii) -7 (iv) -4 .
2. (i) $\frac{3}{4} \quad$ (ii) $\frac{5}{7}$.
3. $x=1, y=-3$.
4. 5. 
1. 64. 
1. (i) $x=3$ (ii) $x=1, y=-1$.

## Chapter Test

1. $x=4, y=3, z=1 ; 2 \frac{1}{40}$. 2. (i) $3 \frac{26}{27} \quad$ (ii) $9 \frac{1}{8}$.
2. (i) $x=6$ (ii) $x=\frac{3}{4}, y=-\frac{8}{3}$
(iii) $x=3, y=\frac{5}{2} \quad$ (iv) $x=3, y=1$

## Exercise 1.1

1. (i) $\log _{5} 25=2$

$$
\text { (ii) } \log _{a} 64=5 \quad \text { (iii) } \log _{7} 100=x
$$

(iv) $\log _{9} 1=0$
(v) $\log _{6} 6=1$
(vii) $\log _{10} 0 \cdot 01=-2$ (viii) $\log _{81} 27=\frac{3}{4}$.
2. (i) $2^{5}=32$
(ii) $3^{4}=81$
(iii) $3^{-1}=\frac{1}{3}$
(iv) $(8)^{\frac{2}{3}}=4$
(v) $(8)^{\frac{5}{3}}=32$
(vi) $10^{-3}=0.001 \quad$ (vii) $2^{-2}=0.25$ (viii) $a^{-1}=\frac{1}{a}$.
3. (i) 4
(ii) 3
(iii) $\frac{3}{2}$
(iv) $\frac{3}{2}$
(v) $-2 \quad$ (vi) -1
(vii) -8 (viii) -2 .
4. (i) 9
(ii) 5
(iii) 0.01
(iv) 2
$\begin{array}{ll}\text { (v) } 11 & \text { (vi) } 4\end{array}$
(vii) 729 (viii) 243
$\begin{array}{lllllll}\text { (ix) } \frac{1}{8} & \text { (x) } 5 & \text { (xi) } 10 & \text { (xii) } 2 & \text { (xiii) } \frac{5}{2} & \text { (xiv) } 2 & \text { (xv) } \pm 3\end{array}$ (vi) $\frac{1}{10}$ (xvii) $6 \frac{1}{2} \quad$ (xviii) $\frac{1}{100}, 1, \sqrt[3]{10}$.
5. $\frac{a^{2}}{1000}$.
(iii) $\frac{x^{2} \sqrt{y}}{z^{3}}$.
7. $10^{a+b}$.
6. (i) $\frac{x^{2}}{1000}$
(ii) $\frac{y^{3}}{10}$
8. $10^{3 m-2 n}$.
(iii) $\frac{x^{3 / 2}}{y^{4}}$.
10. $y^{3} z^{2}$
11. $\frac{x^{4} y^{4}}{100}$.

## Exercise 11.2

1. (i) $\log a$ (ii) $\frac{3}{2}$ (iii) $2 \quad$ (iv) $\log 4$ (v) $6 \quad$ (vi) $\frac{1}{3}$.
2. (i) $\frac{2}{3}$
(ii) $\frac{1}{2} \quad$ (iii) 2
(iv) 1
(v) 2
(vi) 0 (vil
(viii) 2.
3. (i) $\log 27$
(ii) $\log _{10} 8000$
(iii) $\log 256$ (iv) $\log \frac{50}{9} \quad$ (v) $\log 2$
4. $1-4 a+2 b-3 c$.
5. (i) $10^{a}$
(ii) $\frac{2}{5} a$.
6. (i) 0 (ii) 1.
7. (i) $0 \quad$ (ii) 1.
8. $\log _{10}$ 20. 14. $\frac{\sqrt{x}}{\sqrt[3]{y}}$.
9. (i) 1
(ii) 7 .
10. $\frac{4}{3} \pi r^{3}$.
11. 3. 
1. $\frac{100}{x^{2}}$.
2. (i) $\frac{9}{5}$
(ii) 6
(iii) $\frac{3}{2}$
(iv) 1000 .
3. (i) 5 (ii) 1 .
4. (i) 2
(ii) 5
(iii) $4 \cdot 5$
(iv) 3
(v) $1 \quad$ (vi) $14 \quad$ (vii) 2.
5. $1 \frac{1}{40}$.
6. 10 .
7. 3. 
1. $\frac{1}{\alpha+\beta+\gamma}$.
2. (i) 3 (ii) 2 .
3. 4. 

## Chapter Test

1. $\frac{7}{3} \log _{a} x+\frac{8}{3} \log _{a} y-\frac{1}{12} \log _{a} z$.
2. 5. 
1. (i) 7
(ii) $\sqrt{2}$
(iii) $\frac{1}{\sqrt{3}}$
(iv) $6 \frac{1}{2}$
(v) $5,-5$
$\begin{array}{ll}\text { (vi) } 11,-11 & \text { (vii) } 3,-4\end{array}$
(viii) 3 (ix) 10 .
2. $x=1000, y=100$.

## Exercise 12.1

1. (i) Congruent; A.A.S. (ii) Congruent; R.H.S. (iii) Congruent; A.S.A.
(iv) Not necessary ; corresponding sides may not be equal.
2. (i) Congruent; S.A.S. (ii) Not necessary; included angles may not be equal.
(iii) Congruent; A.A.S.
(iv) Congruent; S.S.S.
(v) Congruent; R.H.S.
(vi) Congruent; S.S.S.
(vii) Congruent; R.H.S.
3. (i) $x=15, y=41$
(ii) $x=13, y=11$
(iii) $x=8, y=4$.

## Exercise 12.2

1. (i) 115
(ii) 68
(iii) 12 .
2. (i) 42
(ii) 40
(iii) 93.
3. (a) $x=75^{\circ}, y=75^{\circ}, z=45^{\circ}$
(b) $a=60, b=60, c=65$
(c) $72^{\circ}$.
4. (a) $\angle b=65^{\circ}, \angle d=65^{\circ}$; yes
(b) $135^{\circ}$
(c) $x=127^{\circ}, y=38^{\circ}$.
5. (a) $95^{\circ}$
(b) $74^{\circ}$
(c) $\angle \mathrm{CDE}=52^{\circ}, \angle \mathrm{DCE}=12^{\circ}$.
6. $100^{\circ}$.
7. (a) $\angle \mathrm{ACE}=120^{\circ}, \angle \mathrm{AEC}=30^{\circ}$.
8. (a) $x=20, y=140$
(b) $x=42^{\circ}, y=66^{\circ}, z=48^{\circ}$.

## Exercise 12.3

1. AB .
2. $\angle P$.
3. (i) $\angle \mathrm{C}$
(ii) $\angle \mathrm{A}$.
4. $R P<17.5 \mathrm{~cm}$ and $\mathrm{RP}>2.5 \mathrm{~cm}$.
5. No; $8 \cdot 5+2 \cdot 7<12$.
6. $B C, C A, A B$.
7. $C A, C D, A D$.
8. (a) $\mathrm{AB}, \mathrm{DC}, \mathrm{BD}$
(b) $28^{\circ}$; BD.

## Exercise 12.4

4. $107^{\circ}$ approx. $5 . \mathrm{BC}=3.6 \mathrm{~cm}$, length of perpendicular $=3.1 \mathrm{~cm}$.
5. 8.7 cm .
6. $4.3 \mathrm{~cm}, 5.5 \mathrm{~cm}, 5.5 \mathrm{~cm}$.
7. 3.5 cm .
8. $6 \mathrm{~cm}, 5 \mathrm{~cm}$.
9. $4 \cdot 7 \mathrm{~cm}$.
10. 3.1 cm .
11. 3.9 cm .

## Chapter Test

1. (i) $x=98^{\circ}, y=77^{\circ}$
(ii) $x=108^{\circ}$.
2. (b) (i) 34
(ii) 70
(iii) $44^{\circ}$.
3. (a) $x=46^{\circ}, y=26^{\circ}, z=72^{\circ}$.

## Exercise 13

1. (a) (i) 13 cm
(ii) 8.2 cm
(b) (i) 2.8 cm
(ii) $72^{\circ}$
(c) 5.2 cm .
2. (c) (i) 5 cm
(ii) 10 cm .
3. (i) 3 cm
(ii) 4.6 cm
(iii) 2.4 cm
(iv) 2.2 cm .

## Exercise 14

1. (a) (i) $3: 4$
(ii) $2 \frac{1}{7} \mathrm{~cm}$
(b) $3.2 \mathrm{~cm}, 4.8 \mathrm{~cm}$
(c) $1.5 \mathrm{~cm}, 2.25 \mathrm{~cm}$.
2. (a) $20 \mathrm{~cm}, 4.8 \mathrm{~cm}$
(b) 7.5 cm .
3. (a) $6 \mathrm{~cm}^{2}$
(b) 10 .
4. $10.5 \mathrm{~cm}, 12 \mathrm{~cm}$.
5. (a) $4 \mathrm{~cm}, 10 \mathrm{~cm}$
(b) (ii) $4.8 \mathrm{~cm}, 6 \mathrm{~cm}$
(c) (i) 3 cm
(ii) 4.5 cm .
6. (a) (ii) 2.25 cm
(b) (ii) 10 cm
(c) 16 cm .
7. (a) (ii) 2.9 cm .
8. (b) (ii) $4 \frac{1}{3} \mathrm{~cm} \quad$ (iii) $3: 5$.
$440 \Rightarrow$ UNDERSTANDING ICSE MATHEMATICS - IX
9. (a) $12.5 \mathrm{~cm}, \frac{5}{2} x$ (b) 1.5 cm (c) 22 cm .
10. (b) 6 cm . 15. (b) (i) 15 cm (ii) $\triangle \mathrm{QLP}: \frac{32}{3} \mathrm{~cm}$. 18. 7.8 m .
11. 22.5 m .
12. (a) (i) 9 cm
(ii) 25 cm
(b) $x=2 \frac{13}{16} \mathrm{~cm}, y=5 \mathrm{~cm}$.
13. (a) (ii) $1: 3$
(b) 5 cm .
14. (b) 15 cm .

## Chapter Test

1. (a) $\mathrm{CE}=3 \frac{1}{3} \mathrm{~cm}, \mathrm{DE}=2 \frac{5}{8} \mathrm{~cm}$
(b) $x=5, y=5$
(c) 13.5 cm .

## Exercise 15

1. (i) 13 cm (ii) $2 \sqrt{7} \mathrm{~cm}$ (iii) 8 cm . 2. $16 \mathrm{~cm}, 12 \mathrm{~cm}$. 4. $10 \mathrm{~m}, 24 \mathrm{~m}, 26 \mathrm{~m}$.
2. $4 \sqrt{3} \mathrm{~cm}, 16 \sqrt{3} \mathrm{~cm}^{2}$. $6.8 \sqrt{2} \mathrm{~cm}, 32 \sqrt{2} \mathrm{~cm}^{2}$.
3. $50 \mathrm{~cm}^{2}, 20 \sqrt{2} \mathrm{~cm}$.
4. (a) 4 cm
(b) $5 \sqrt{2} \mathrm{~cm}, 25 \mathrm{~cm}^{2}$.
5. (a) 13 cm
(b) 17 cm
(c) $3 \frac{1}{6} \mathrm{~cm}$.
6. (a) $4 \mathrm{~cm}, 8 \mathrm{~cm}, 20 \mathrm{~cm}, 5 \sqrt{17} \mathrm{~cm}$.
7. 13 cm .
8. 100 cm .
9. (a) 12 cm (b) 26 cm (c) (ii) $24 \mathrm{~cm}^{2}, 14 \sqrt{2} \mathrm{~cm}$.
10. (a) $12 \mathrm{~cm}, 6 \sqrt{3} \mathrm{~cm}$
(b) 36 cm
(c) (i) 13 cm
(ii) $\mathrm{EF}=7.8 \mathrm{~cm}, \mathrm{BF}=7.2 \mathrm{~cm}$.

## Chapter Test

1. (a) 28 cm (b) (i) 10 cm (ii) 24 cm (iii) $96 \mathrm{~cm}^{2}$
(c) (i) 12 cm (ii) $13.5 \mathrm{~cm}^{2}$.
2. $\mathrm{DC}=4.5 \mathrm{~cm}, \mathrm{AC}=7.5 \mathrm{~cm}$.
3. 60 cm .
4. (i) 8 cm (ii) 14 cm (iii) 22 cm .
5. $3 \sqrt{2} \mathrm{~cm}$.

## Exercise 16.1

1. (i) $900^{\circ}$ (ii) $1440^{\circ}$ (iii) $1800^{\circ}$.
2. (i) $120^{\circ}$ (ii) $135^{\circ}$ (iii) $156^{\circ}$.
3. (i) 10 (ii) 9 (iii) 8 (iv) 7 .
4. (i) 5 (ii) 18 (iii) 8 (iv) 11 .
5. (i) 16 (ii) 21 (iii) 10 .
6. (i) Yes (ii) No (iii) No.
7. (i) Yes (ii) Yes (iii) No.
8. (i) No (ii) No (iii) Yes.
9. (i) $40^{\circ}$ (ii) 9. 10. $x=36^{\circ}, y=36^{\circ}, z=72^{\circ}$. 11. 6 .
10. 14. 
1. $84^{\circ}$.
2. $60^{\circ}, 90^{\circ}, 150^{\circ}, 60^{\circ}$; one.
3. $80^{\circ}, 100^{\circ}, 120^{\circ}, 140^{\circ}, 100^{\circ}$.
4. 92. 
1. 61 .
2. 50 .
3. 123 .
4. 11 .
5. 69 .
6. $\angle C=100^{\circ}, \angle D=120^{\circ}$.
7. $\angle \mathrm{BCD}=128^{\circ}, \angle \mathrm{E}=80^{\circ}$.
8. 8. 
1. (i) 5 (ii) 9 (iii) 20 .
2. (i) 5 (ii) 7 (iii) 9 .
3. 6 and 8 .
4. 5,10 .
5. $\angle \mathrm{EAP}=72^{\circ}, \angle \mathrm{BPA}=108^{\circ}$.

## Exercise 16.2

1. $90^{\circ}, 120^{\circ}$.
2. $54^{\circ}, 90^{\circ}, 108^{\circ}, 108^{\circ}$.
3. $72^{\circ}, 108^{\circ}, 72^{\circ}, 108^{\circ}$.
4. (a) $\angle \mathrm{CDB}=30^{\circ}, \angle \mathrm{ADB}=80^{\circ}$
(b) $\angle \mathrm{OAD}=35^{\circ}, \angle \mathrm{AOD}=68^{\circ}, \angle \mathrm{ADO}=77^{\circ}$ (c) $x=54$.
5. (a) $x=4, y=5$ (b) $x=30^{\circ}, y=95^{\circ} \quad$ (c) $x=6, y=21 . \quad$ 15. $80^{\circ}$.
6. (a) $45^{\circ} \quad$ (b) $\angle \mathrm{OAB}=\angle \mathrm{OBA}=34^{\circ}, \angle \mathrm{AOB}=112^{\circ}$
(c) $\angle \mathrm{OAD}=54^{\circ}, \angle \mathrm{ADO}=36^{\circ}, \angle \mathrm{AOD}=90^{\circ}$.
7. (a) $x=50^{\circ}, y=88^{\circ} \quad$ (b) $x=36^{\circ}, y=108^{\circ} \quad$ (c) $\angle \mathrm{ODC}=58^{\circ}, \angle \mathrm{OBA}=34^{\circ}$.
8. $\sqrt{3}: 1$.

## Exercise 16.3

1. $63^{\circ}$.
2. 7.2 cm .
3. $5 \cdot 6 \mathrm{~cm}$.
4. $6 \cdot 1 \mathrm{~cm}$.
5. $3 \cdot 1 \mathrm{~cm}$.
6. $61^{\circ}$.
7. 3.5 cm .
8. $106^{\circ}$.
9. $78^{\circ}$.

## Chapter Test

1. 26. 
1. 12. 
1. $120^{\circ}$.
2. (i) $x=29^{\circ}$ (ii) $x=39^{\circ}, y=111^{\circ}$ (iii) $x=64^{\circ}, y=96^{\circ}$.
3. (i) $x=37^{\circ}, y=106^{\circ}, z=37^{\circ}$
(ii) $x=110^{\circ}$
(iii) $x=70^{\circ}, y=120^{\circ}, z=85^{\circ}$.
4. (i) $17^{\circ}$
(ii) $73^{\circ}$
(iii) $45^{\circ}$
(iv) $73^{\circ}$.
5. $8 \mathrm{~cm}, 8 \sqrt{3} \mathrm{~cm}$.

## Exercise 17

10. (b) $5: 9$ (c) (i) $2: 1$ (ii) $1: 6$.
11. (a) 5 cm
(b) 6 units
(c) (i) $18 \mathrm{~cm}^{2}$
(ii) AEFD.
12. (a) (i) $40 \mathrm{~cm}^{2} \quad$ (ii) $120 \mathrm{~cm}^{2}$.
13. (a) $\mathrm{AB}=12 \mathrm{~cm}, \mathrm{BC}=9 \mathrm{~cm}$
(b) $\mathrm{BC}=12 \mathrm{~cm}, \mathrm{CA}=10 \mathrm{~cm}, \mathrm{AB}=15 \mathrm{~cm}$
$\begin{array}{ll}\text { (c) (i) } 80 \mathrm{~cm}^{2} & \text { (ii) } 5: 3 \text {. }\end{array}$
14. 25 sq. units.

## Exercise 18.1

1. $12 \mathrm{~cm}^{2}$.
2. (i) $6 \mathrm{~cm}^{2}$
(ii) $210 \mathrm{~cm}^{2}$
(iii) $34.56 \mathrm{~cm}^{2}$.
3. $336 \mathrm{~cm}^{2} ; 33.6 \mathrm{~cm}$.
4. Rs 47250 .
5. $30 \mathrm{~cm}^{2}, 30 \mathrm{~cm}$.
6. $27.71 \mathrm{~m}^{2}$.
7. 54 cm .
8. $62.4 \mathrm{~cm}^{2} ; 10.4 \mathrm{~cm}$.
9. (i) $96 \mathrm{~cm}^{2}$ (ii) $2598 \mathrm{~m}^{2}$.
10. $8 \mathrm{~cm}^{2} ; 2.83 \mathrm{~cm}$.
11. $34 \cdot 86 \mathrm{~cm}^{2}$.
12. $12 \mathrm{~cm}^{2}$.
13. 17 cm .
14. 40 cm .
15. $150 \mathrm{~cm}^{2}$.
16. $210 \mathrm{~cm}^{2} ; 70 \mathrm{~cm}$.
17. Base $=16 \mathrm{~cm}$, each of other sides $=12 \mathrm{~cm}$.
18. 24 cm or 10 cm .
19. $1200 \mathrm{~m}, 400 \mathrm{~m}$.
20. (a) $19.3 \mathrm{~cm}^{2}$ (b) $12.5 \mathrm{~cm}^{2}$.

## Exercise 18.2

1. (i) $240 \mathrm{~cm}^{2}$ (ii) $108 \mathrm{~cm}^{2}$.
2. $306 \mathrm{~m}^{2}$.
3. $92 \cdot 35 \mathrm{~cm}^{2} .4 .84 \mathrm{~cm}^{2}$.
4. $30 \mathrm{~cm}, 540 \mathrm{~cm}^{2}$.
5. 98 m .
6. (a) $400 \mathrm{~m}^{2}$ (b) $28 \mathrm{~cm}^{2}$.
7. $160 \mathrm{~m}^{2}$.
8. (i) $26 \mathrm{~m}, 10 \mathrm{~m}$
(ii) $100 \mathrm{~m}^{2}$.
9. 3 m .
10. $8000 \mathrm{~m}^{2}$.
11. $960 ; \frac{7}{20}$.
12. $16 x=5 y ; 60 \mathrm{~m}^{2}$.
13. $x^{2}+13 x-30=0, x=2$ metres.
14. $75 \cdot 6 \mathrm{~m}^{2}$.
15. $278 \mathrm{~m}^{2}$.
16. (a) $23 \mathrm{~m}, 17 \mathrm{~m}^{2}$
(b) $50 \mathrm{~m}, 51 \mathrm{~m}^{2}$
(c) $50 \mathrm{~cm}^{2}, 54 \mathrm{~cm}$.
17. 8 cm .
18. $22 \mathrm{~m}, 31 \cdot 11 \mathrm{~m}$.
19. $196 \mathrm{~m}^{2}, 19.80 \mathrm{~m}$.
20. (i) $81 \mathrm{~cm}^{2}$ (ii) $80 \mathrm{~cm}^{2}$.
21. $119.8 \mathrm{~cm}^{2}, 11.98 \mathrm{~cm}$.
22. $\frac{p q}{p+q r} \mathrm{~cm}$.
23. $96 \mathrm{~cm}^{2}$.
24. 20 cm .
25. $120 \mathrm{~cm}^{2}, 12 \mathrm{~cm}$.
26. $18 \mathrm{~cm}^{2}$.
27. $96 \mathrm{~cm}^{2}$.
28. $7.5 \mathrm{~cm}^{2}$.
29. (a) $5 \mathrm{~cm}, 26 \mathrm{~cm}^{2}$ (b) 8 units, 40 sq. units (c) $2 \cdot 4 \mathrm{~m} .34 .216 \mathrm{~cm}^{2}$.
30. 14 cm .
31. $90 \mathrm{~cm}^{2}$.
32. $35 \mathrm{~cm}, 25 \mathrm{~cm}$.
33. 40 cm .
34. Base $=14 \mathrm{~cm}$, altitude $=7 \mathrm{~cm}$.
35. $24 \mathrm{~m}, 12 \mathrm{~m}$.
36. $240 \mathrm{~m}^{2}$.
37. 96 cm .
38. 48 cm .
39. $(130+32 \sqrt{3}) \mathrm{cm}^{2}, 4(8+5 \sqrt{2}) \mathrm{cm}$. 43. (a) $51 \cdot 59 \mathrm{~cm}^{2}$ (b) $32 \mathrm{~cm}^{2}$ (c) $192 \mathrm{~cm}^{2}$.
40. (a) $4.5 \mathrm{~m}^{2}$ (b) $1087.5 \mathrm{~m}^{2}$ (c) $72 \mathrm{~cm}^{2}$.
41. 40 metres.
42. 12 cm
43. $\frac{105}{x} \mathrm{~cm}, 44=2\left(x+\frac{105}{x}\right) ; 15 \mathrm{~cm}, 7 \mathrm{~cm}$.
44. $(90-x) \mathrm{m} ; x(90-x)=1800 ; 60 \mathrm{~m}, 30 \mathrm{~m}$.

## Exercise 18.3

1. (i) 44 cm ; $154 \mathrm{~cm}^{2}$ (ii) $132 \mathrm{~cm} ; 1386 \mathrm{~cm}^{2}$ (iii) $22 \mathrm{~cm} ; 38.5 \mathrm{~cm}^{2}$.
2. $346.5 \mathrm{~m}^{2}$.
3. 8.8 m .
4. 40216 km .
5. 14 cm .
6. $9 \mathrm{~cm} ; 81 \pi \mathrm{~cm}^{2}$.
7. $12 \mathrm{~cm} ; 24 \pi \mathrm{~cm}$.
8. 105.6 m .
9. 5000 .
10. (i) 44 cm
(ii) $154 \mathrm{~cm}^{2}$
(iii) $42 \mathrm{~cm}^{2}$.
11. $126 \mathrm{~cm}^{2}$.
12. $33 ; 28 \cdot 38 \mathrm{~cm}^{2}$.
13. $962 \cdot 5 \mathrm{~m}^{2}$.
14. $88 \mathrm{~m}^{2}$.
15. 14 cm .
16. 17.5 cm .
17. $2618 \mathrm{~m}^{2}$; ₹ 130900 .
18. $346.5 \mathrm{~cm}^{2}, 154 \mathrm{~cm}^{2}$.
19. 44 cm .
20. 44 m .
21. (i) 22 cm
(ii) $77 \mathrm{~cm}^{2}$.
22. $77 \mathrm{~cm}^{2}$.
23. (i) $38 \mathrm{~cm} ; 50.75 \mathrm{~cm}^{2}$ (ii) $88 \mathrm{~cm} ; 504 \mathrm{~cm}^{2}$.
24. $44 \mathrm{~cm} ; 42 \mathrm{~cm}^{2}$.
25. (i) 88 cm
(ii) $308 \mathrm{~cm}^{2}$.

## Exercise 18.4

1. $294 \mathrm{~cm}^{2}, 343 \mathrm{~cm}^{3}$.
2. $94 \mathrm{~m}^{2} ; 60 \mathrm{~m}^{3} ; 7.07 \mathrm{~m}$.
3. 14 cm .
4. 40 ; 6 .
5. (a) 12 cm
(b) $150 \mathrm{~cm}^{2}, 125 \mathrm{~cm}^{3}$.
6. 7
7. 70 cm .
8. $486 \mathrm{~cm}^{2}, 15 \cdot 57 \mathrm{~cm}$.
9. 9 cm .
10. $504000 \mathrm{~cm}^{3} ; 38200 \mathrm{~cm}^{2}$.
11. 120. 
1. 60 .
2. $0.729 \mathrm{~m}^{3} ; 0.9 \mathrm{~m}$.
3. 7.39 cm
4. $38 \mathrm{~cm}^{3}$.
5. (a) $1440 \mathrm{~cm}^{2}$
(b) $6 \mathrm{~cm} ; 1: 2$.
6. 3 cm .
7. ₹ 12480 .
8. 13.95 cm .
9. $\frac{8}{13}$ metre.
10. ₹ 1350 .
11. ₹ $2596 \cdot 80$.
12. 75 cm .
13. 6 cm .
14. 8.4 litres.
15. (a) $80 \mathrm{~cm}^{3}$ (b) (i) $16.5 \mathrm{~m}^{2}$ (ii) $6600 \mathrm{~m}^{3}$ (c) $1000 \mathrm{~m}^{3}$. 27. $2250 \mathrm{~m}^{3}$.

## Exercise 18.5

1. $150 \pi \mathrm{~cm}^{2}$.
2. (i) $13200 \mathrm{~cm}^{2}$
(ii) $115 \cdot 5$ litres.
3. $4620 \mathrm{~cm}^{3} ; 1260 \mathrm{~cm}^{3}$.
4. $616 \mathrm{~cm}^{3}$.
5. (i) $62 \frac{6}{7} \mathrm{~m}^{3}$
(ii) ₹ $6285 \cdot 70$.
6. 2000.7. $112 \pi \mathrm{~cm}^{2} ; 240 \pi \mathrm{~cm}^{2}$.8. 49.5 kg .
7. (i) 40 cm (ii) $38500 \mathrm{~cm}^{3}$.10. (i) 15.9 cm(ii) $4998.9 \mathrm{~cm}^{3}$.
8. 45100.12. $22: 15$.13. $1: 2$.14. 30 cm ; $4620 \mathrm{~cm}^{3}$.15. $1078 \mathrm{~cm}^{3}$.16. $16: 9$.17. 31.2 cm .18. $3 \frac{19}{77} \mathrm{~cm}$.
9. 60.20. 30 cm .21. (i) 1155 litres(ii) 24 minutes.22. $\frac{1}{6}$ minutes.23. $5: 3$.24. $306.24 \mathrm{~cm}^{3}$.25. (i) $968 \mathrm{~cm}^{2}$(ii) $1064 \cdot 8 \mathrm{~cm}^{2}$(iii) $2038.08 \mathrm{~cm}^{2}$.
10. Wood : $5.28 \mathrm{~cm}^{3}$; graphite : $0.11 \mathrm{~cm}^{3}$27. Cylinder by $85 \mathrm{~cm}^{3}$.
11. $1478 \cdot 4 \mathrm{~kg}$.29. 3.6 m .
12. $74 \cdot 1 \mathrm{~cm}$.
13. $22 \mathrm{~cm}^{2}$.

## Chapter Test

1. (a) $54 \mathrm{~cm}^{2}$
(b) 32 cm .
2. $529.89 \mathrm{~cm}^{2}$.
3. (a) $51 \mathrm{~cm}^{2}$
(b) $144 \mathrm{~cm}^{2}$
(c) $54 \mathrm{~m}^{2}$.
4. $19.3 \mathrm{~cm}^{2}$.
5. $31 \cdot 4 \mathrm{~cm}$.
6. $196 \mathrm{~cm}^{2}$
7. ₹ 20790.
8. $1480 \cdot 5 \mathrm{~m}^{2}$.
9. $59.4 \mathrm{~cm} ; 61 \cdot 1 \mathrm{~cm}^{2}$.
10. No.
11. 378 km .
12. 75 cm .
13. (i) 8 cm (ii) $448 \mathrm{~cm}^{3}$.
14. $152000 \mathrm{~cm}^{3} ; 16800 \mathrm{~cm}^{2}$.
15. (i) $564000 \mathrm{~cm}^{3}$ (ii) $69864 \mathrm{~cm}^{3} \quad$ (iii) 55.9 kg .
16. (i) 450 (ii) ₹ 54000 .
17. ₹ 756.
18. $44 \mathrm{~m}^{2}$.
19. $30 \cdot 69$ hours (approx.)
20. ₹ 29700 .
21. 22 cm .
22. $162 \mathrm{~cm}^{3}$.
23. $7 \mathrm{~cm} ; 5 \mathrm{~cm}$
24. $\frac{7}{19} \mathrm{~cm}$.

## Exercise 19

1. (a) (i) $\frac{3}{5}$
(ii) $\frac{4}{5}$
(iii) $\frac{3}{4}$
(iv) $\frac{4}{3}$
(v) $\frac{5}{4}$
(vi) $\frac{5}{3}$
(b) (i) $\frac{5}{13}$
(ii) $\frac{12}{13}$
(iii) 1
(iv) 1 .
2. (a) (i) $\frac{4}{5}$
(ii) $\frac{4}{5}$
(iii) $\frac{7}{5}$
(iv) 1
(b) (i) $\frac{5}{12}$
(ii) $\frac{4}{5}$
(iii) 1 (iv) 14 .
3. (a) (i) $\frac{4}{5}$
(ii) $\frac{3}{4}$
(iii) -1
(iv) $\frac{3}{2 \sqrt{2}}$
(v) -1
(b) $\left(\right.$ i) $\frac{2}{3}$
(ii) $\frac{2}{\sqrt{13}}$ (iii) 1 .
4. (a) (i) $\frac{2}{5}$
(ii) $\frac{2}{5}$
(iii) $\frac{6}{5}$
(iv) $\frac{1 \dot{4}}{5}$
(b) $(i) \frac{3}{5}$
(ii) 4 units.
5. (i) $\frac{12}{13}$
(ii) $\frac{1}{5}$.
6. (a) (i) $\frac{7}{25}$
(ii) $\frac{24}{7}$
(b) $\left(\right.$ i) $\frac{9}{41}$
$\begin{array}{lll}\text { (ii) } \frac{40}{41} & \text { (iii) } \frac{40}{9}\end{array}$
7. (i) $\frac{3}{5}$ (ii) $\frac{4}{5}$.
8. (a) (i) $\frac{4}{5}$
(ii) $\frac{4}{3}$
(iii) $\frac{7}{12}$
(b) $4 \frac{4}{5}$
(c) (i) $\mathrm{AD}=20 \mathrm{~cm}, \mathrm{AB}=25 \mathrm{~cm}, \mathrm{DC}=20 \mathrm{~cm}, \mathrm{AC}=20 \sqrt{2} \mathrm{~cm}$.
9. (i) $\frac{4}{5}$
(ii) $\frac{3}{4}$. 10. $\frac{5}{13} ; \frac{12}{13}$.
10. $1 \frac{11}{20}$.
11. $1 \frac{2}{5}$.
12. $\frac{2(\sqrt{5}-1)}{\sqrt{5}}$.
13. $\frac{p+\sqrt{q^{2}-p^{2}}}{q}$.
14. $3 \frac{31}{120}$.
15. $\frac{12}{65}$.
16. 8. 
1. $\frac{3}{5}$.
2. $2 \frac{3}{7}$.
3. $\frac{17}{19}$.
4. $\frac{p^{2}-q^{2}}{p^{2}+q^{2}}$.
5. $\frac{1}{9}$.
6. (i) $\frac{17}{19}$ (ii) 3 .
7. $\frac{1}{4}$.
8. $\frac{3}{2}$.
9. (a) (i) $\frac{6}{5}$
(ii) $\frac{5}{13}$
(b) (i) $\frac{12}{13}$ (ii) $\frac{5}{12}$.
10. $\frac{150}{\sqrt{13}} \mathrm{~cm} ; 103 \frac{11}{13} \mathrm{~cm}^{2}$.
11. (a) (i) $\frac{5}{13}$
(ii) $\frac{4}{3}$
(b) $\frac{12}{\sin \theta}$ or $\frac{9}{\cos \theta}$.
12. $\cot \theta$.
13. 2. 

## Chapter Test

1. (a) $\sin \mathrm{A}=\frac{2}{3}, \cos \mathrm{~A}=\frac{\sqrt{5}}{3}, \tan \mathrm{~A}=\frac{2}{\sqrt{5}}, \cot \mathrm{~A}=\frac{\sqrt{5}}{2}, \sec \mathrm{~A}=\frac{3}{\sqrt{5}}$, $\operatorname{cosec} A=\frac{3}{2} ; \sin C=\frac{\sqrt{5}}{3}, \cos C=\frac{2}{3}, \tan C=\frac{\sqrt{5}}{2}, \cot C=\frac{2}{\sqrt{5}}$, $\sec C=\frac{3}{2}, \operatorname{cosec} C=\frac{3}{\sqrt{5}}$.
(b) $x=10 \cot \theta, y=10 \operatorname{cosec} \theta$.
2. (a) (i) $\frac{4}{5}$
(ii) $3 \frac{2}{15}$
(b) (i) 3
$\begin{array}{ll}\text { (ii) } 5 \frac{1}{4} & \text { (iii) }-4 \frac{3}{4}\end{array}$
3. $\frac{q^{2}-2 p^{2}}{p \sqrt{q^{2}-p^{2}}}$.
4. (i) $\frac{3}{5}$
(ii) $\frac{4}{5}$
(iii) -1 .
5. $\frac{3}{5}$.
6. $9 \frac{1}{9}$.
7. $12 \frac{8}{15} \mathrm{~m}$.

## Exercise 20.1

1. (i) $\frac{7}{4}$
(ii) 2
(iii) $\frac{3}{2}$
(iv) $\frac{1}{4}$.
2. (i) $\frac{1}{3}$
(ii) $\frac{3}{2}$
(iii) $\frac{25}{36}$.
3. (i) 0
(ii) 3 (iii) $-5 \frac{17}{20}$.
4. (i) $\frac{1}{\sqrt{3}}$
(ii) $\frac{1}{3}$.
5. $2: \sqrt{3}$.
6. $60^{\circ}$.
7. $45^{\circ} ; \frac{3}{2}$.
8. (i) $\sqrt{3}$
(ii) 60
(iii) $\frac{1}{2}$
(iv) 2.
9. (i) $30^{\circ}$ (ii) $20^{\circ}$ (iii) $15^{\circ}$ (iv) $30^{\circ}$.
10. $15^{\circ}$.
11. (i) 60
(ii) 1 (iii) $-\frac{1}{2}$.
12. (i) $45^{\circ}$
(ii) $45^{\circ}$.
13. (i) $\frac{1}{2}$
(ii) $\frac{1}{2}$
(iii) -1 . 19. $\frac{1}{2}$.
14. $60^{\circ}$.
15. $\mathrm{A}=45^{\circ}, \mathrm{B}=15^{\circ}$.
16. (i) $90^{\circ}$ or $60^{\circ}$
(ii) $30^{\circ}$ or 15
(iii) $60^{\circ}$ or $15^{\circ}$.
17. $8 \mathrm{~cm}, 8 \sqrt{3} \mathrm{~cm}$.
18. $2 \sqrt{3} \mathrm{~cm}, 4 \sqrt{3} \mathrm{~cm}$.
19. $12 \sqrt{3} \mathrm{~m}$.
20. $4(3-\sqrt{3}) \mathrm{m}$.

## Exercise 20.2

1. (i) 1 (ii) $\frac{1}{2}$.
2. (i) 0
(ii) 0 .
3. (i) 0
(ii) 1 .
4. (i) $0 \quad$ (ii) 1 .
5. (i) $\frac{2}{3}$
(ii) $\frac{7}{4}$.
6. $\frac{2}{3}$.
7. $\frac{3}{\sqrt{13}}$.

## Chapter Test

1. (i) $1 \frac{1}{4}$
(ii) 1
(iii) $3 \frac{1}{2}$.
2. $\frac{4}{3}$.
3. (i) $45^{\circ}, 30^{\circ}$
(ii) $10^{\circ}, 22 \frac{1}{2}^{\circ}$.
4. $\mathrm{A}=52 \frac{1}{2}^{\circ}, \mathrm{B}=7 \frac{1}{2}^{\circ}$.
5. (i) 5
(ii) -1 .
6. $6 \sqrt{3} \mathrm{~cm}$.

## Exercise 21.1

1. $(i)(3,-4)$
(ii) $\left(-\frac{3}{2}, 5\right)$
(iii) $\left(-1 \frac{2}{3},-2 \frac{1}{4}\right)$
(iv) $(-2,5)$
(v) $(-2,0) \quad$ (vi) $\left(0, \frac{3}{2}\right)$.
2. $\mathrm{A}(2,2), \mathrm{B}(-3,0), \mathrm{C}(-2,-4), \mathrm{D}(3,-1), \mathrm{E}(-4,4), \mathrm{F}(0,-2), \mathrm{G}(2,-3), \mathrm{H}(0,3)$.
3. A lies in the first quadrant, B lies on $x$-axis, C lies in the third quadrant and D in the fourth quadrant.
4. (i) collinear (ii) non-collinear (iii) collinear.
5. $\mathrm{M}(-3,0)$ and $\mathrm{N}(0,4)$.
6. Rectangle; 15 sq. units.
7. Rhombus; 12 sq. units.
8. $(2,-2) ; 25$ square units.
9. $(0,0),(6,0),(6,4),(0,4)$.
10. $(0,0),(-6,0),(-6,-4),(0,-4)$.
11. $\mathrm{O}(0,0), \mathrm{A}(a, \sqrt{3} a), \mathrm{B}(2 a, 0)$.

## Exercise 21.2

4. (i) $m=2, c=0$ (ii) $m=-5, c=0$. 5. (i) $m=-3, c=0$ (ii) $m=\frac{3}{2}, c=0$.
5. (i) $m=-\frac{5}{3}, c=0$ (ii) $m=-\frac{2}{5}, c=0$
6. (i) $m=2, c=3$ (ii) $m=-1, c=-1$.
7. (i) $m=-3, c=5$
(ii) $m=5, c=7$.
8. (i) $m=-1, c=\frac{3}{2}$ (ii) $m=-\frac{1}{2}, c=-\frac{1}{2}$.
9. (i) $m=\frac{2}{3}, c=\frac{5}{3}$ (ii) $m=-\frac{3}{4}, c=3$.
10. (i) $m=\frac{5}{3}, c=-2$ (ii) $m=-\frac{4}{3}, c=\frac{7}{3}$ (iii) $m=0, c=\frac{4}{5}$.
11. $(-3,0),(0,2)$.
12. (i) $0,8 \quad$ (ii) $0,-6$.
13. (i) parallel
(ii) not parallel
(iii) parallel.
14. (i) $(-2,5)$, perpendicular
(ii) $(1,1)$, perpendicular.
15. 28 sq. units.

## Chapter Test

1. $-2 ; 15$ sq. units. $\quad$ 2. $(4,-1) ;(i)(3,7) \quad$ (ii) $(4,3) \quad$ (iii) $(3,3) ; 16$ sq. units.
2. $(-1,3) ;(-1,0) ; 24$ sq. units.
3. (i) $m=2, c=-1$ (ii) $m=-\frac{2}{3}, c=2$ (iii) $m=\frac{2}{3}, c=-\frac{4}{3} .5 .6 ;-\frac{5}{3}$.
4. (i) $1,45^{\circ}, 2$
(ii) $\sqrt{3}, 60^{\circ}, 5$
(iii) $\frac{1}{\sqrt{3}}, 30^{\circ},-\frac{4}{\sqrt{3}}$.
5. (i) -6
(ii) 8 .
6. $(2,-1)$; not perpendicular.

## Exercise 22.1

1. 6. 
1. 13 hours.
2. 2780 .
3. $6 \cdot 5$.
4. (i) $\frac{41}{6}$ (ii) $10 \frac{5}{7}$.
5. (i) 82 (ii) Vijay: 12 years, Rahul : 15 years; Rakhi : 18 years. 7. 8.
6. 18. 
1. 13. 
1. 45.9 kg .
2. 42. 
1. 5. 
1. Mean $=2 \cdot 4$, median $=2 \cdot 5$.
2. Mean time $=25$ minutes, media time $=24$ minutes.
3. Mean $=54 \cdot 8$, median $=52$.
4. Mean $=15 \cdot 5$ points, median $=12$ points.
5. 45. 
1. 11. 

## Exercise 22.2

1. (i) Discrete (ii) continuous (iii) discrete (iv) continuous (v) continuous.

| 2. Classes | $0-4$ | $5-9$ | $10-14$ | $15-19$ | $20-24$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 2 | 7 | 8 | 6 | 2 |

3. (i)

| Classes | $1-10$ | $11-20$ | $21-30$ | $31-40$ |
| :--- | :---: | :---: | :---: | :---: |
| Frequency | 8 | 7 | 6 | 6 |

(ii) Range $=38$ (iii) $25 \cdot 5$.
5. (i) frequency
(ii) size
(iii) 14
(iv) class mark
(v) $6 \cdot 5$.

6. (i) | Classes | $1-10$ | $11-20$ | $21-30$ | $31-40$ | $41-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 8 | 7 | 10 | 8 |

(ii) Classes $10 \cdot 5-10 \cdot 5 ~ 10 \cdot 5-20 \cdot 5 ~ 20 \cdot 5-30 \cdot 5 ~ 30 \cdot 5-40 \cdot 5) ~ 40 \cdot 5-50 \cdot 5$
(iii) lower limit $=20 \cdot 5$; upper limit $=30 \cdot 5$
(iv) 35.5 .
7. (i) upper limit $=52$; lower limit $=48$
(ii) upper limit $=52 \cdot 5$; lower limit $=47.5$
(iii) $37 \cdot 5$ and $42 \cdot 5$
(iv) 45
(v) 5.

8. Marks \% | $10-19$ | $20-29$ | $30-39$ |
| :---: | :---: | :---: |

| Marks \% <br> (classes) | $10-19$ | $20-29$ | $30-39$ | $40-49$ | $50-59$ | $60-69$ | $70-79$ | $80-89$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 11 | 20 | 46 | 57 | 37 | 15 | 7 |
| C. frequency | 7 | 18 | 38 | 84 | 141 | 178 | 193 | 200 |

9. 

| Classes | $0-10$ | $10-20$ | $20-30$ | $30-40$ | $40-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 5 | 5 | 7 | 10 | 8 |
| C. frequency | 5 | 10 | 17 | 27 | 35 |

Number of students obtaining below 20 marks $=10$.
10. (i)

| Classes | Tally marks | Frequency | Cumulative frequency |
| :---: | :---: | :---: | :---: |
| $0-10$ | III | 3 | 3 |
| $10-20$ | II | 2 | 5 |
| $20-30$ | $\mathbb{N N}$ NN I | 11 | 16 |
| $30-40$ | $\mathbb{N N}$ NN III | 18 | 34 |
| $40-50$ | - | - | 34 |
| $50-60$ | III | 3 | 37 |
| $60-70$ | II | 2 | 39 |
| $70-80$ | III | 3 | 42 |
| $80-90$ | $\mathbb{N N}$ | 5 | 47 |
| $90-100$ | III | 3 | 50 |

(ii) $30-40$
(iii) 34
(iv) 13.

11. | Classes | $0-4$ | $4-7$ | $7-10$ | $10-13$ | $13-16$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 7 | 31 | 137 | 73 | 52 |

Number of children in the age group $10-13=73$.

12. | Classes | $0-10$ | $11-20$ | $21-30$ | $31-40$ | $41-50$ | $51-60$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 2 | 5 | 11 | 14 | 11 | 7 |
13. Classes $|$|  | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ | $100-110$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |

|  | Frequency | 2 | 1 | 4 | 4 | 9 | 5 | 3 |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |

14. 

| Classes | $23 \cdot 5-27.5$ | $27 \cdot 5-31 \cdot 5$ | $31 \cdot 5-35 \cdot 5$ | $35 \cdot 5-39 \cdot 5$ | $39 \cdot 5-43 \cdot 5$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 | 7 | 4 | 4 | 11 |

15. (i) 10 ; lower limit $=119$; upper limit $=129$
(ii) 7 ; lower limit $=20$; upper limit $=27$.

## Exercise 22.3

17. Class intervals | $30-40$ | $40-50$ | $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ | $100-110$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of houses | 3 | 1 | 4 | 5 | 9 | 3 | 3 | 4 |
18. Clac|c|c|c|c|c | Class intervals | $40-42$ | $42-44$ | $44-46$ | $46-48$ | $48-50$ |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Frequency | 2 | 12 | 7 | 6 | 7 |
19. (i) 18
(ii) $475-500$
(iii) 34
(iv)

| Classes | Frequency | Cumulative frequency |
| :---: | :---: | :---: |
| $375-400$ | 6 | 6 |
| $400-425$ | 18 | 24 |
| $425-450$ | 10 | 34 |
| $450-475$ | 20 | 54 |
| $475-500$ | 4 | 58 |

## Chapter Test

1. Mean $=4 \cdot 25$, median $=4 \cdot 5 . \quad$ 2. Mean $=12 \cdot 4$, median $=7$.
2. 51 kg .
3. 14.6 years.
4. 10 .
5. $150 \cdot 25 \mathrm{~cm}$.
6. $35 \cdot 5$.
7. 62. 
1. Class intervals

| $50-60$ | $60-70$ | $70-80$ | $80-90$ | $90-100$ | $100-110$ | $110-120$ | $120-130$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 2 | 6 | 5 | 8 | 5 | 7 | 3 | 4 |

13. Class intervals $|$| Cl 20 | $21-22$ | $23-24$ | $25-26$ | $27-28$ | $29-30$ |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| No. of students | 3 | 5 | 10 | 10 | 5 | 2 |
14. 

(i) 6
(ii) $45-51$
(iii) $51-57$

| Classes | $27-33$ | $33-39$ | $39-45$ | $45-51$ | $51-57$ | $57-63$ |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Frequency | 4 | 12 | 18 | 6 | 20 | 8 |

